



Pavel
Panchekha



University
of Utah

Automated Reasoning for Web Page Layout

Formally proving pages accessible:

- Specifying visual properties
- Formalizing browser rendering
- Overcoming solver limitations
- Finding modularity in web pages

2019-07-msr

View Zoom Add Slide Play Keynote Live Table Chart Text Shape Media Comment Collaborate Format Animate Document

HC Get 2019 health coverage. Hes: X +

https://www.healthcare.gov

HealthCare.gov Español Log in

Get Coverage Keep or Update Your Plan See Topics - Get Answers **SEARCH**

2019 Open Enrollment is over. Still need health insurance?

You can enroll in or change plans if you have certain life changes, or qualify for Medicaid or CHIP.

SEE IF I CAN ENROLL **SEE IF I CAN CHANGE**

Looking for coverage for a small business? [Learn more](#)

NEED TO SUBMIT DOCUMENTS? **SEE HOW**

Transitions

No Transition Effect

Add an Effect

Start Transition Delay

On Click 0.50 s

Build Order



2019-07-msr



Firefox

System tray icons: Activity Dashboard, Spotlight, Keynote, Firefox, Photos, App Store, Print, Trash

HealthCare.gov

Español

Login

Get Coverage

Keep or Update Your Plan

See Topics

Get Answers

Search

SEARCH

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How We Find Layout Bugs

Build Order

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2019-07-msr



Firefox

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On Click 0.50 s



2019-07-msr



Firefox

Layout Bugs are Endemic



HealthCare.gov
Missing button



Bank of America
Hidden text



FAFSA
Overlapping text



Walgreens
Hidden tabs

Layout Bugs are Endemic



HealthCare.gov
Missing button



Bank of America
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FAFSA
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Bank of America
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Walgreens
Hidden tabs

12% of Americans have disabilities

Layout Bugs are Endemic



HealthCare.gov
Missing button



Bank of America
Hidden text



FAFSA
Overlapping text



Walgreens
Hidden tabs

12% of Americans have disabilities

Accommodation legally required (under ADA)

How We Find Layout Bugs

Industry standard:

Manual Testing



Manual review
of renderings

Manual selection
of configurations

How We Find Layout Bugs

Industry standard:

Manual Testing



Manual review
of renderings

Manual selection
of configurations

State of the Art:

Automated Tests



Auto-comparison
of renderings

Random test array
of configurations

How We Find Layout Bugs

Industry standard:
Manual Testing



Manual review
of renderings

Manual selection
of configurations

State of the Art:
Automated Tests



Auto-comparison
of renderings

Random test array
of configurations

My Work:
Verification



Formal specification
for valid renderings

Automated proof
for all configurations

How VizAssert Works

How VizAssert Works

Formalize

Accessibility



Equations

Web Page



How VizAssert Works

Formalize

Solve

Accessibility



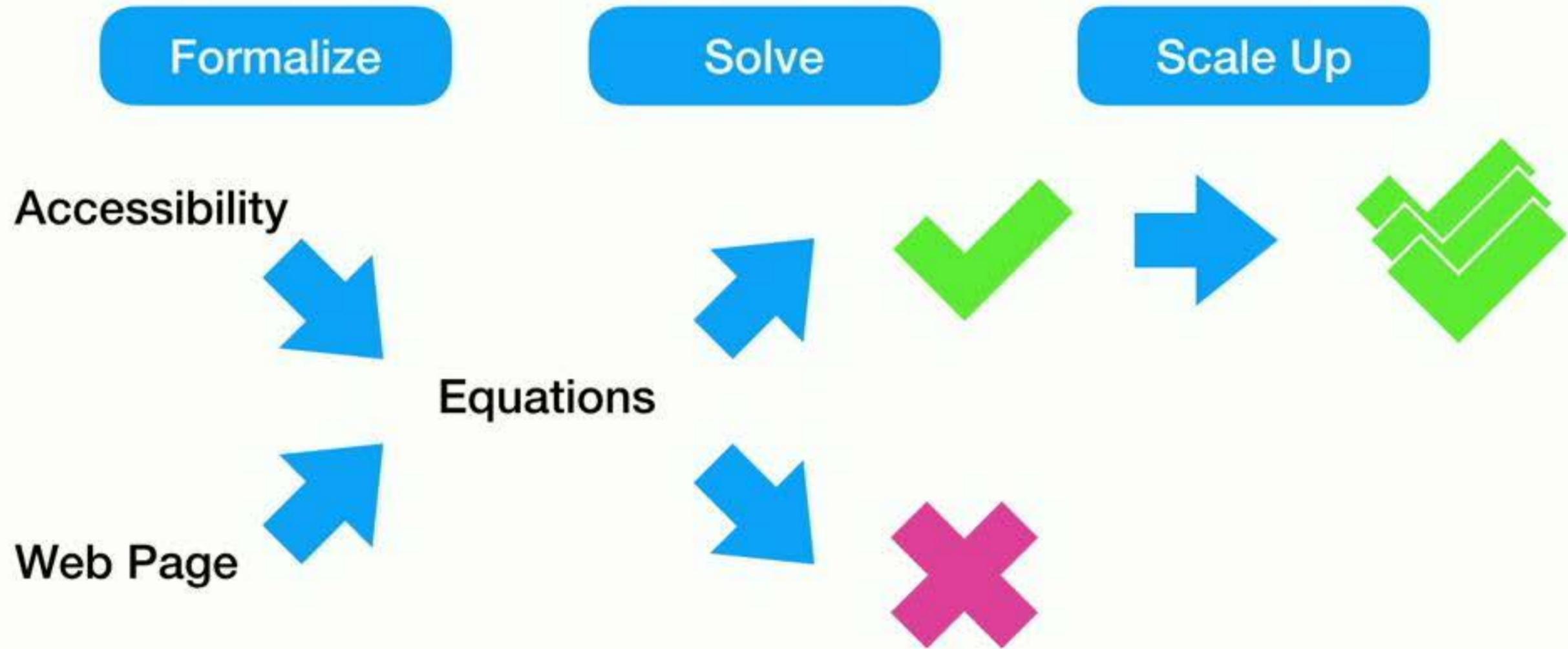
Equations



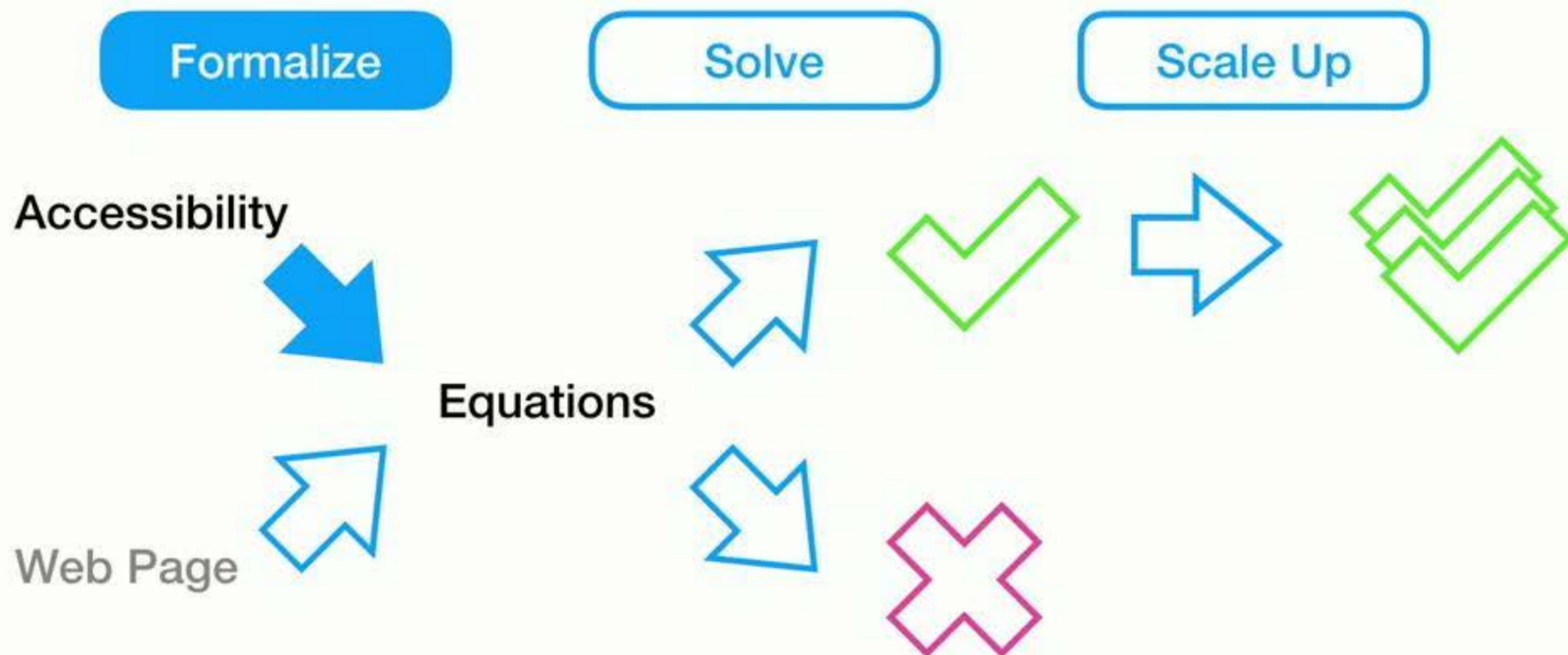
Web Page



How VizAssert Works



How VizAssert Works



Web Pages



HTML + CSS + JS

Web Pages



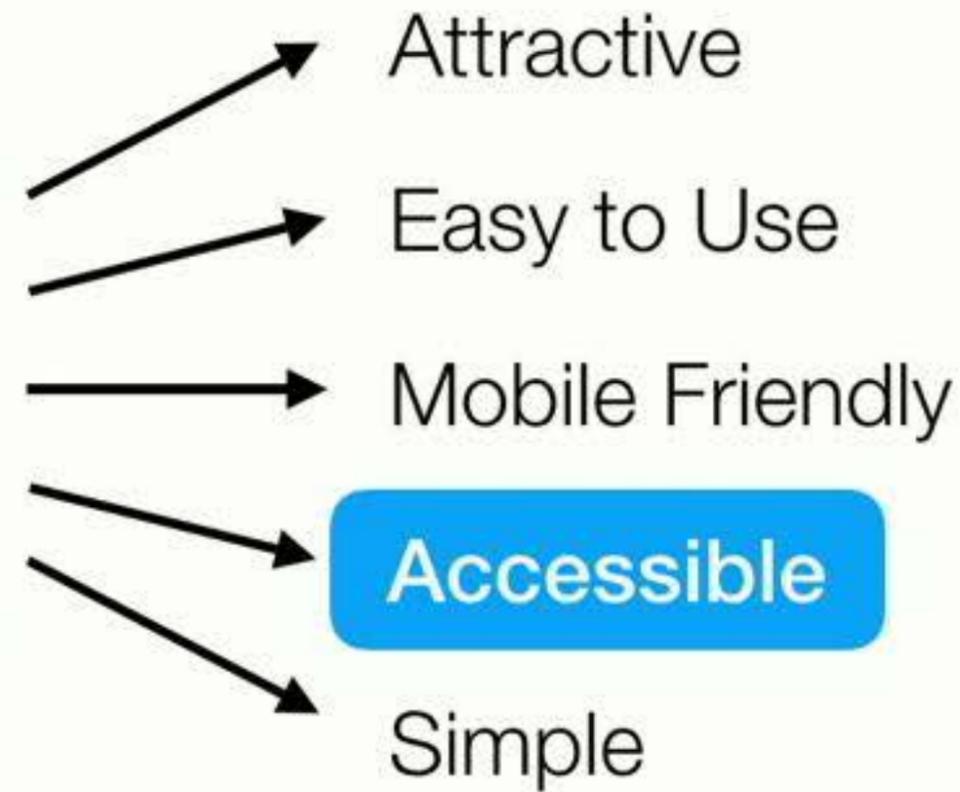
HTML + CSS

- Attractive
- Easy to Use
- Mobile Friendly
- Accessible
- Simple

Web Pages



HTML + CSS



Accessibility Guidelines

Developed by
accessibility researchers

Accessibility Guidelines

Developed by
accessibility researchers

All handled by VizAssert

Size & position guidelines

- Text is at least 14px tall
- Lines are at most 80 chars
- Text doesn't overlap

Screen-reader assistance

- Screen-reader text is offscreen
- Header hierarchy matches sizes

Functionality guidelines

- Text zoom up to 200%
- Scrolling in only one dimension

Accessibility Guidelines

Developed by
accessibility researchers

Select page elements

All handled by VizAssert

Size & position guidelines

- Text is at least 14px tall
- Lines are at most 80 chars
- Text doesn't overlap

Screen-reader assistance

- Screen-reader text is offscreen
- Header hierarchy matches sizes

Functionality guidelines

- Text zoom up to 200%
- Scrolling in only one dimension

Accessibility Guidelines

Developed by
accessibility researchers

Select page elements

Constrain geometry

All handled by VizAssert

Size & position guidelines

- Text is at least 14px tall
- Lines are at most 80 chars
- Text doesn't overlap

Screen-reader assistance

- Screen-reader text is offscreen
- Header hierarchy matches sizes

Functionality guidelines

- Text zoom up to 200%
- Scrolling in only one dimension

Accessibility Guidelines

Guideline

Text zoom up to 200%
with same functionality



HealthCare.gov
Missing button

Accessibility Guidelines

Guideline

Text zoom up to 200%
with same functionality



Behavior

The search bar
and search button
must be inside
the toolbar
(for text zoom ≤ 2)



HealthCare.gov
Missing button

Accessibility Guidelines

Guideline

Text zoom up to 200%
with same functionality



Behavior

The search bar
and search button
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the toolbar
(for text zoom ≤ 2)



HealthCare.gov
Missing button

Formal Specifications

Behavior

The search bar
and search button
must be inside
the toolbar
(for text zoom ≤ 2)



HealthCare.gov
Missing button

Formal Specifications

Behavior

CSS Selector

`div[role=banner] [type]`

must be inside

`#header + div + div`

(for text zoom ≤ 2)

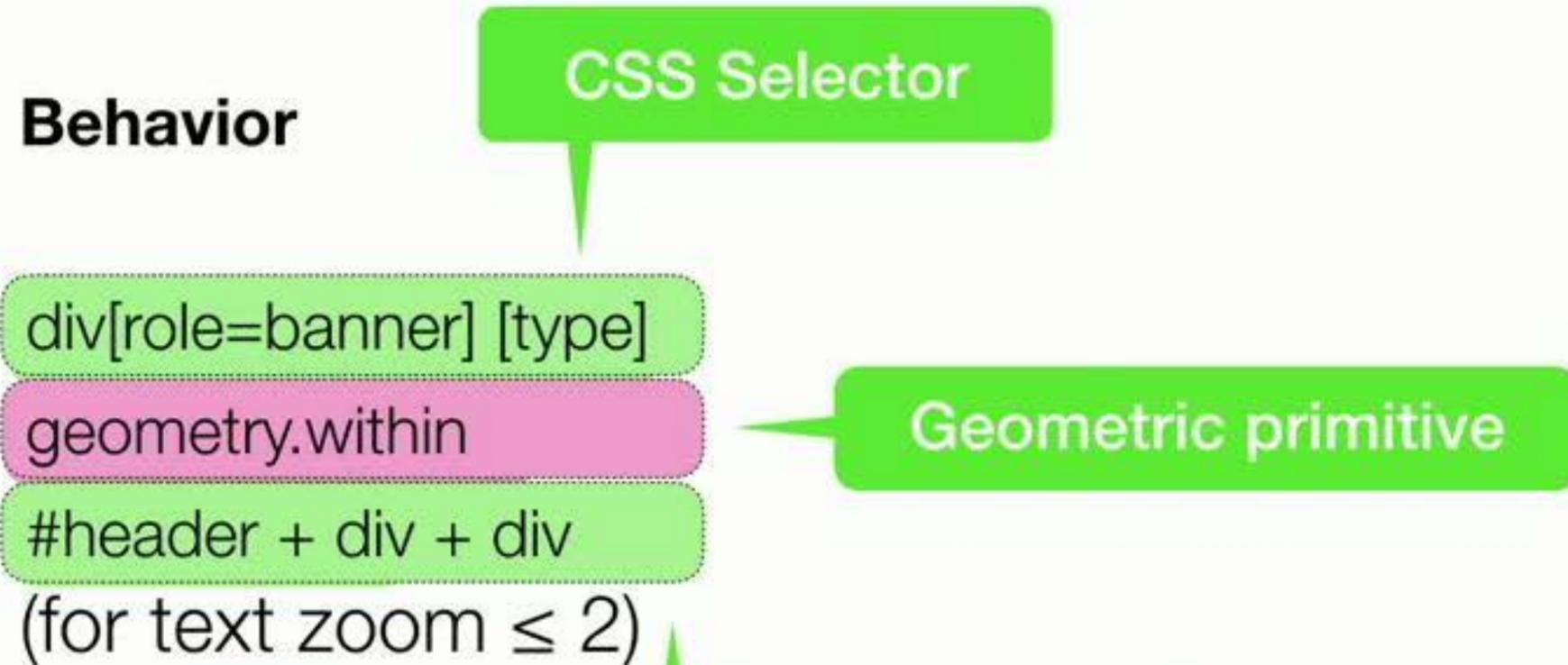


CSS Selector

HealthCare.gov

Missing button

Formal Specifications



HealthCare.gov
Missing button

Formal Specifications

Behavior

The search bar
and search button
must be inside
the toolbar
(for text zoom ≤ 2)



HealthCare.gov
Missing button

Formalize
→

Visual Logic

all elements matching
`div[role=banner] [type]`
are `geometry.within`
the `#header + div + div`
when `text.zoom $\leq 200\%$`

Formal Specifications

Behavior

The search bar
and search button
must be inside
the toolbar
(for text zoom ≤ 2)



HealthCare.gov
Missing button

Formalize
→

Visual Logic

all elements matching
`div[role=banner] [type]`
are `geometry.within`
the `#header + div + div`
when `text.zoom $\leq 200\%$,`
`window.width ≥ 800`

Only on desktop

Specification to Equations

Visual Logic

all elements matching

`div[role=banner] [type]`

are `geometry.within`

the `#header + div + div`

when `text.zoom ≤ 200%`,
`window.width ≥ 800`

Specification to Equations

Visual Logic

all elements matching

`div[role=banner] [type]`

are `geometry.within`

the `#header + div + div`

when `text.zoom ≤ 200%`,
`window.width ≥ 800`



Equations over Renderings

`within(B, A) =`

`B.left ≥ A.left &&`

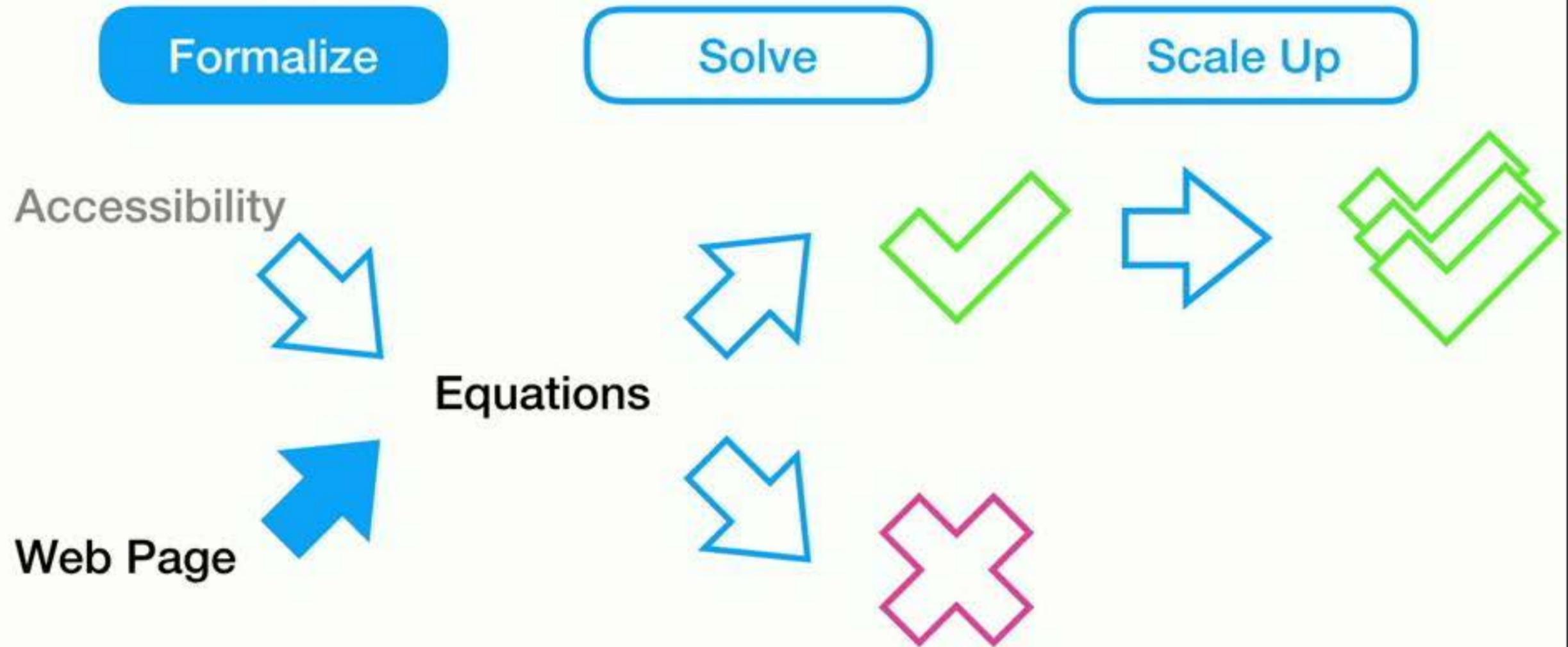
`B.top ≥ A.top &&`

`B.left + B.width ≤ A.left + A.width &&`

`B.top + B.height ≤ A.top + A.height`

Sizes & positions
of elements

How VizAssert Works



Web Browser

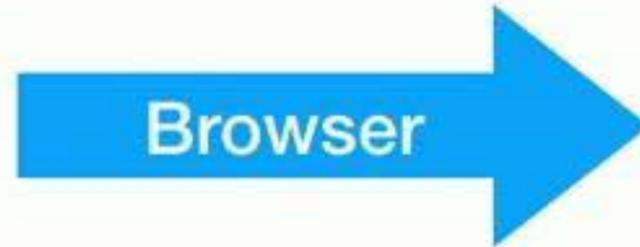
Web Page

HTML + CSS

Configuration

Size: 1920x1280

Text zoom: 1.5x



Rendering



Web Browser

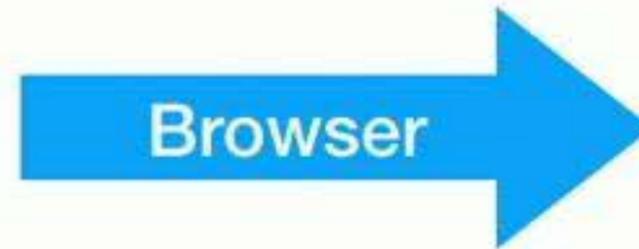
Web Page

HTML + CSS

Configuration

Size: 1920x1280

Text zoom: 1.5x



Rendering



Web Browser

Modern Web Browsers:

Millions of lines of code

Decades of development

Dozens of developers

Rendering



Symbolic Web Browser

Web Page

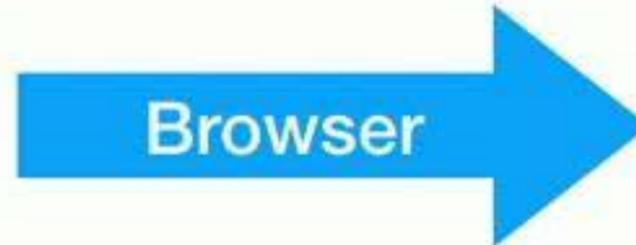
HTML + CSS

Configuration

Size: $W \times H$

Text zoom: $Z\times$

Symbolic



Rendering



Symbolic Web Browser

Web Page

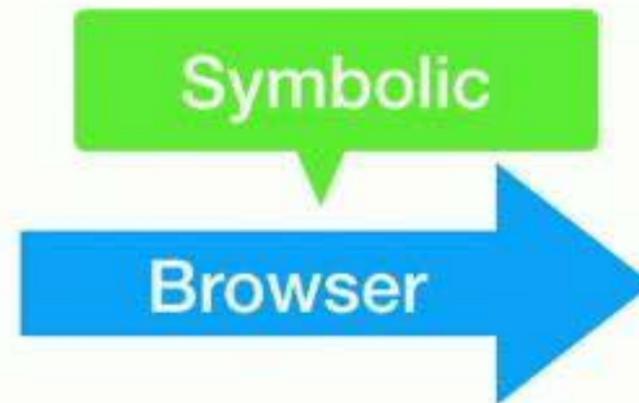
HTML + CSS

Configuration

Size: $W \times H$

Text zoom: $Z\times$

Symbolic



Rendering



Symbolic Web Browser

Web Page

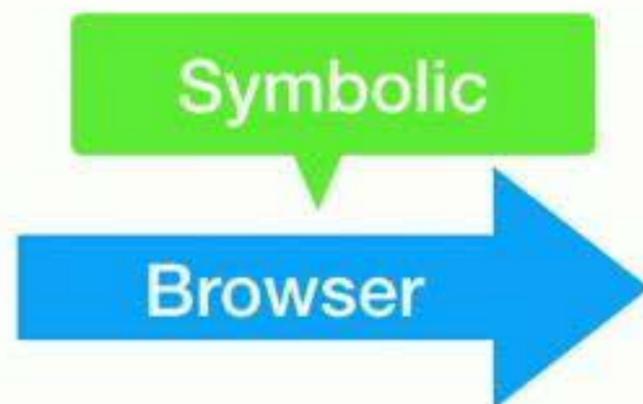
HTML + CSS

Configuration

Size: $W \times H$

Text zoom: $Z\times$

Symbolic



Rendering

Symbolic



Sizes & positions
depend on W, H, Z

Symbolic Web Browser

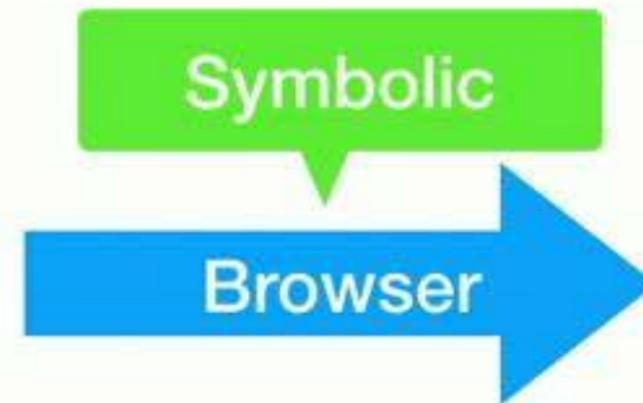
Web Page

HTML + CSS

Configuration

Size: $W \times H$

Text zoom: $Z\times$



Rendering



Problem: write a symbolic web browser

Symbolic Web Browser

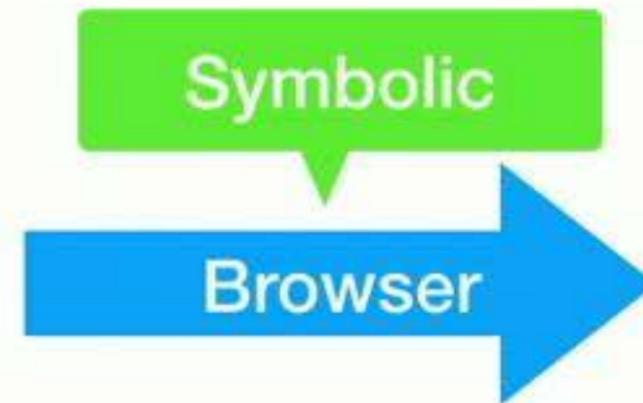
Web Page

HTML + CSS

Configuration

Size: $W \times H$

Text zoom: $Z\times$



Rendering



Problem: write a symbolic web browser



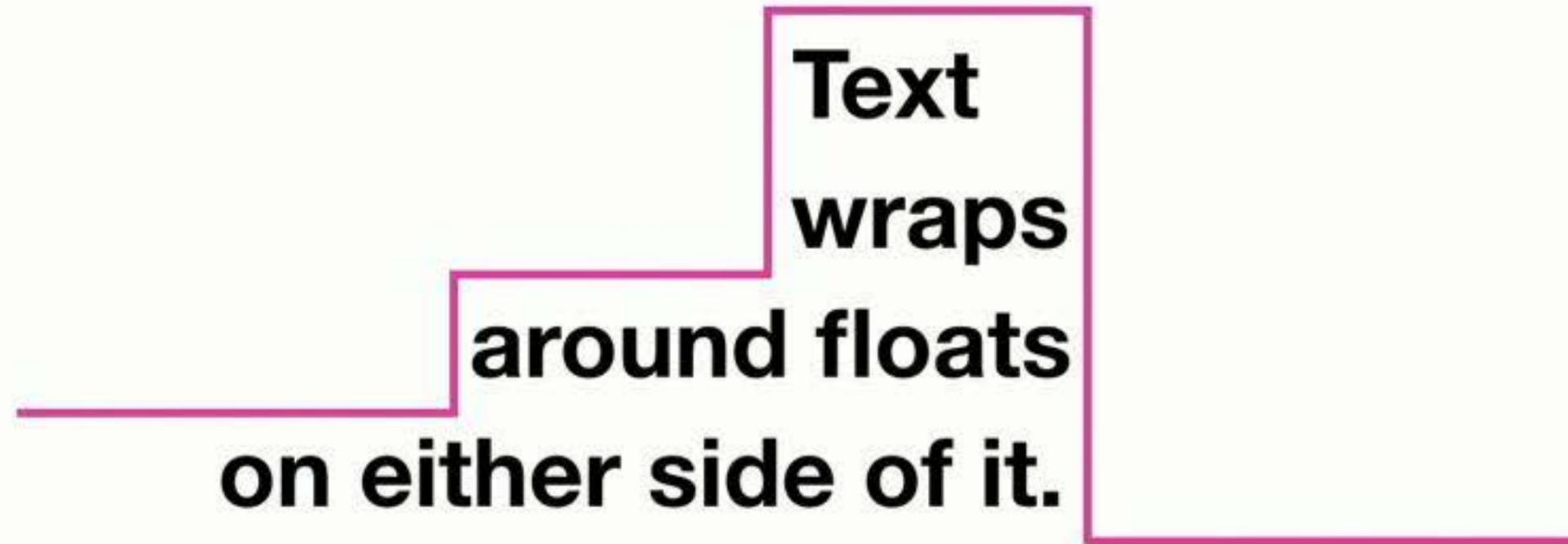
Encodings for visual properties

Scaling symbolic reasoning

Encoding Visual Props



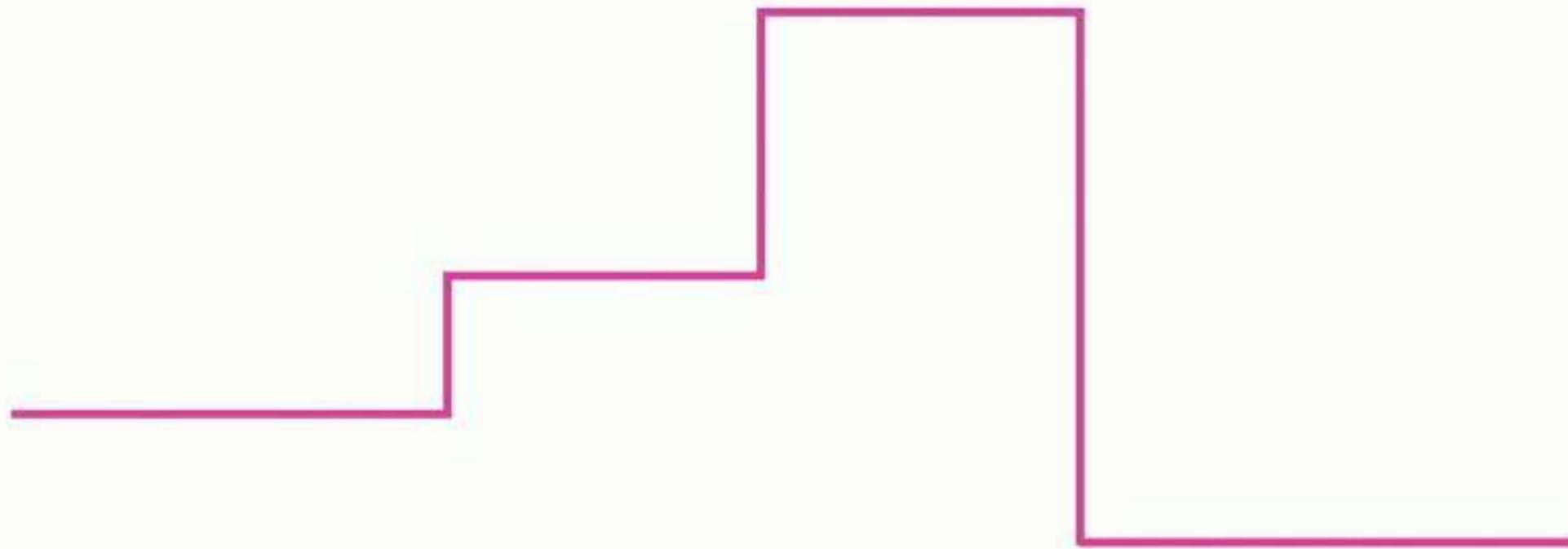
Encoding Visual Props



“Exclusion zone” data structure

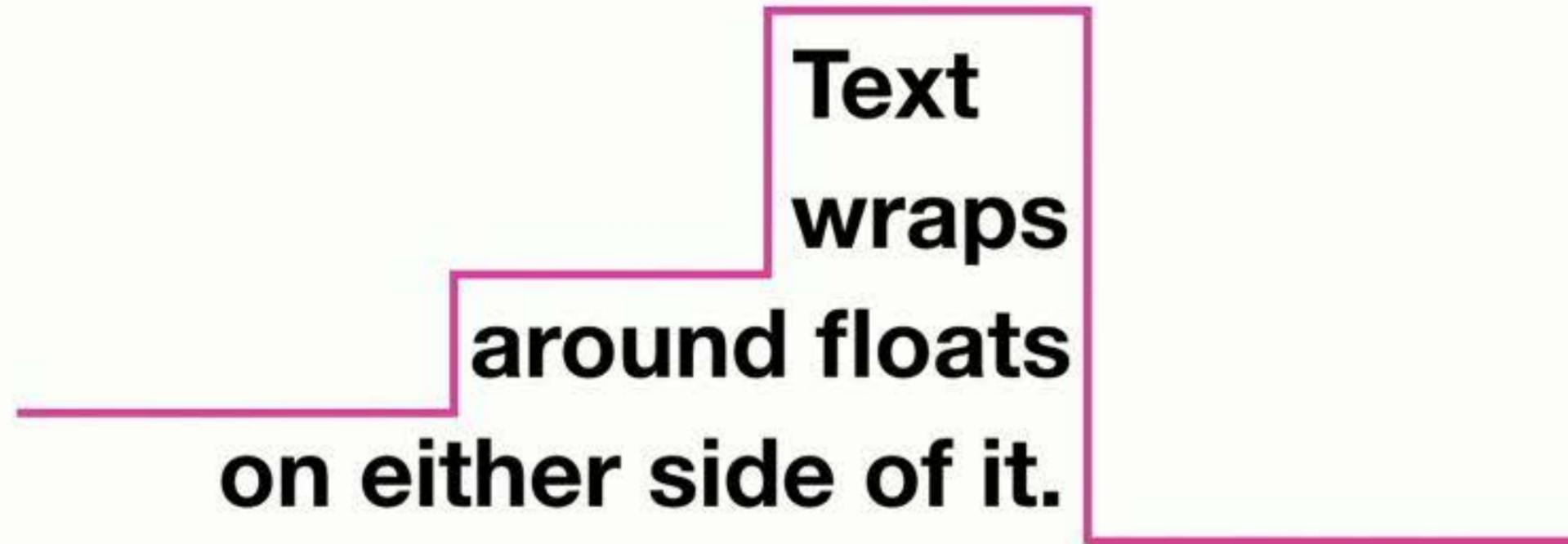
Encoding Visual Props

Encoding Visual Props



`ezone.add(size, position)`

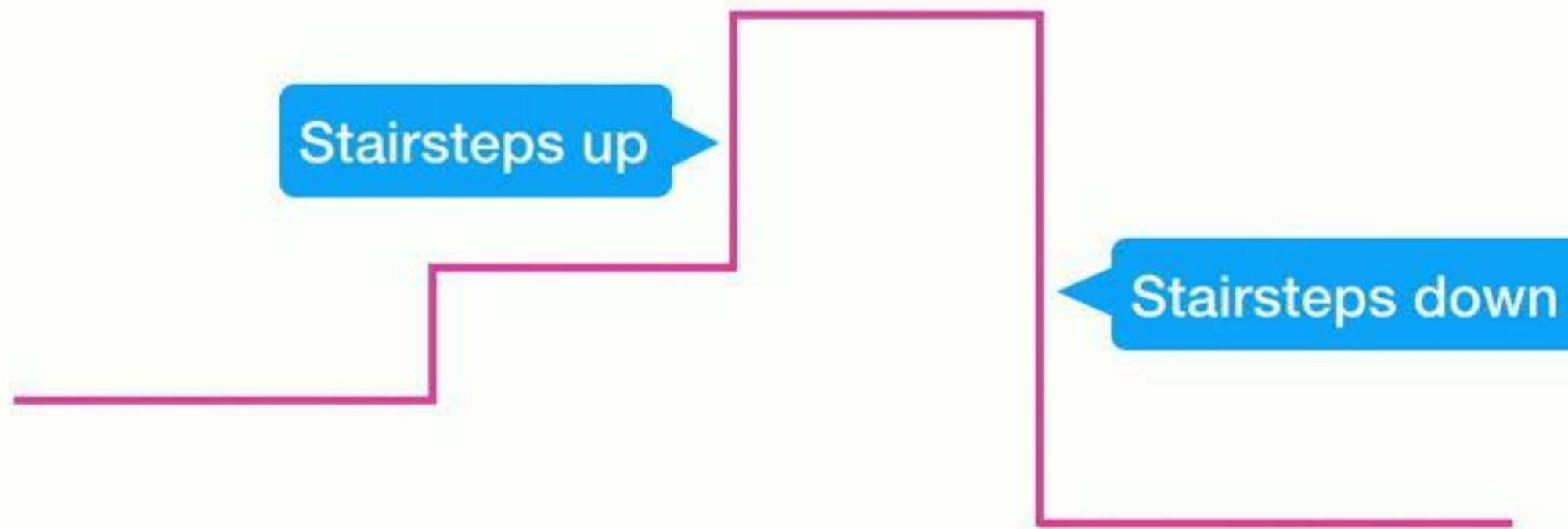
Encoding Visual Props



ezone.**add**(size, position)

ezone.**place**(size) → position

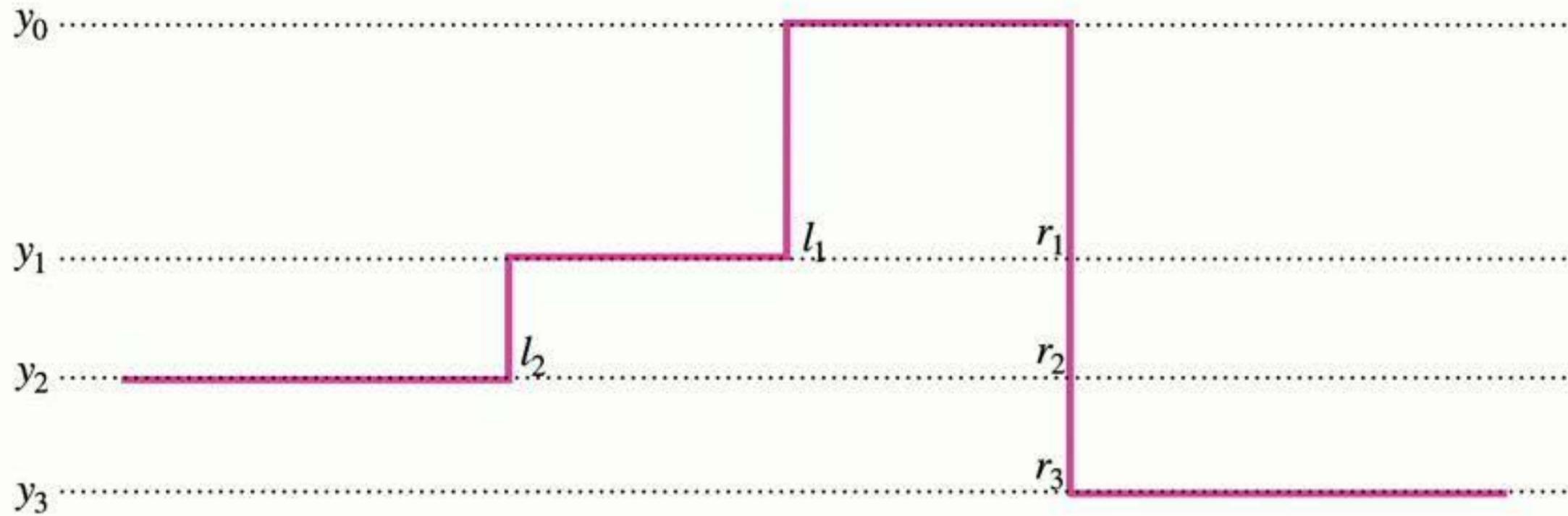
Encoding Visual Props



ezone.**add**(size, position)

ezone.**place**(size) → position

Encoding Visual Props



`ezone.add(size, position)`

`ezone.place(size) → position`

Encoding Visual Props

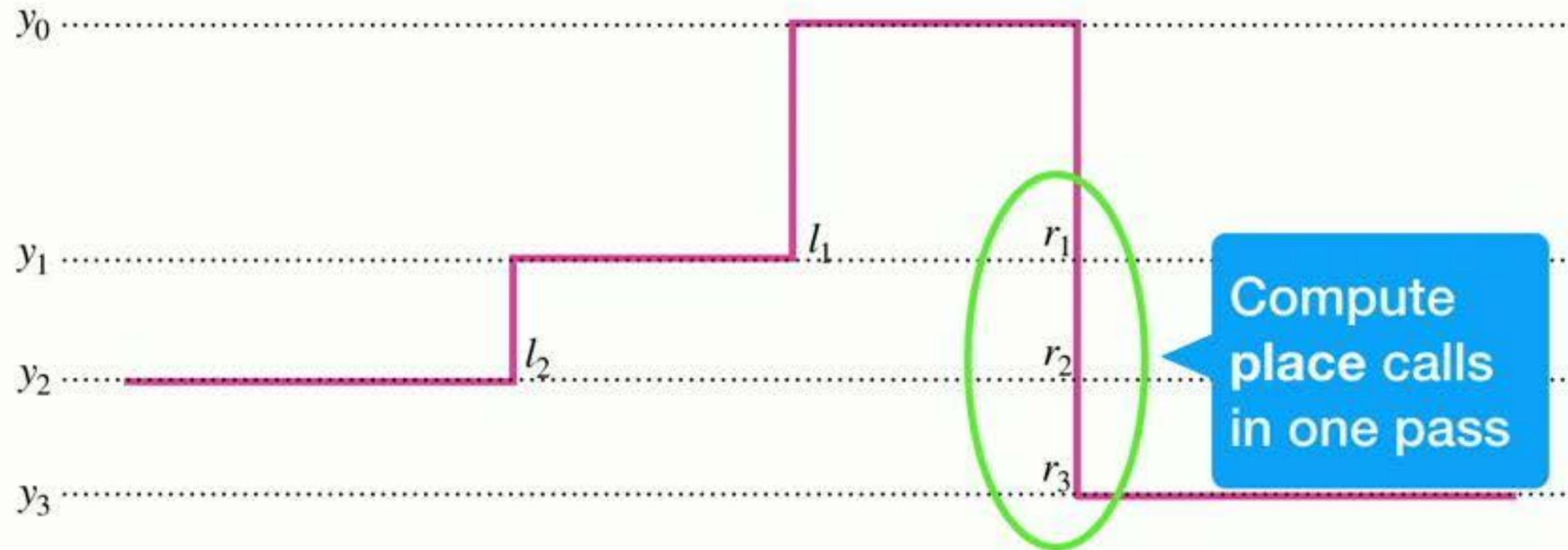


`ezone = y0 (y1, l1, r1) (y2, l2, r2) (y3, \perp , r3)`

`ezone.add(size, position)`

`ezone.place(size) → position`

Encoding Visual Props

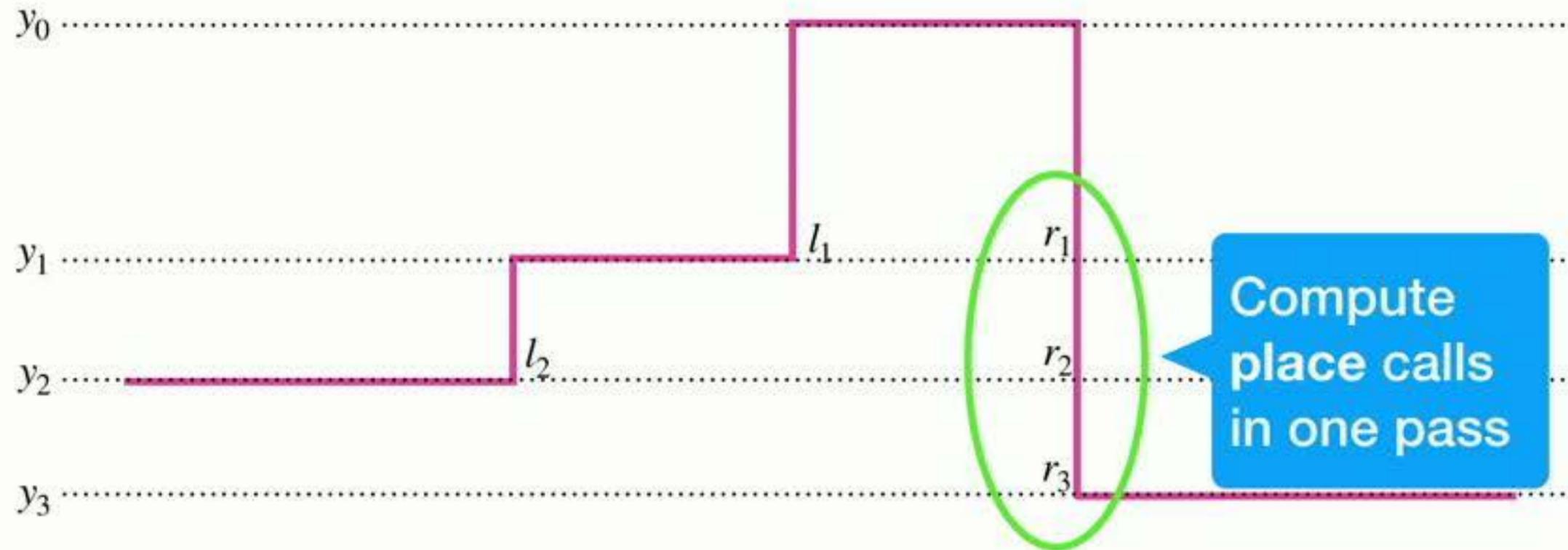


`ezone = y0 (y1, l1, r1) (y2, l2, r2) (y3, \perp , r3)`

`ezone.add(size, position)`

`ezone.place(size) \rightarrow position`

Encoding Visual Props



ezone = y_0 (y_1, l_1, r_1) (y_2, l_2, r_2) (y_3, \perp, r_3)

ezone.**add**(size, position)

$O(n)$ equations

ezone.**place**(size) \rightarrow position

$O(n)$ equations

Validating the Formalization

Validating the Formalization

Standard Tests



Validating the Formalization

Non-automated

Standard Tests

W3C[®]

Validating the Formalization

Non-automated

Standard Tests



Browsers



Validating the Formalization

Non-automated

Standard Tests



Browsers



Evaluate: Differential testing vs browsers

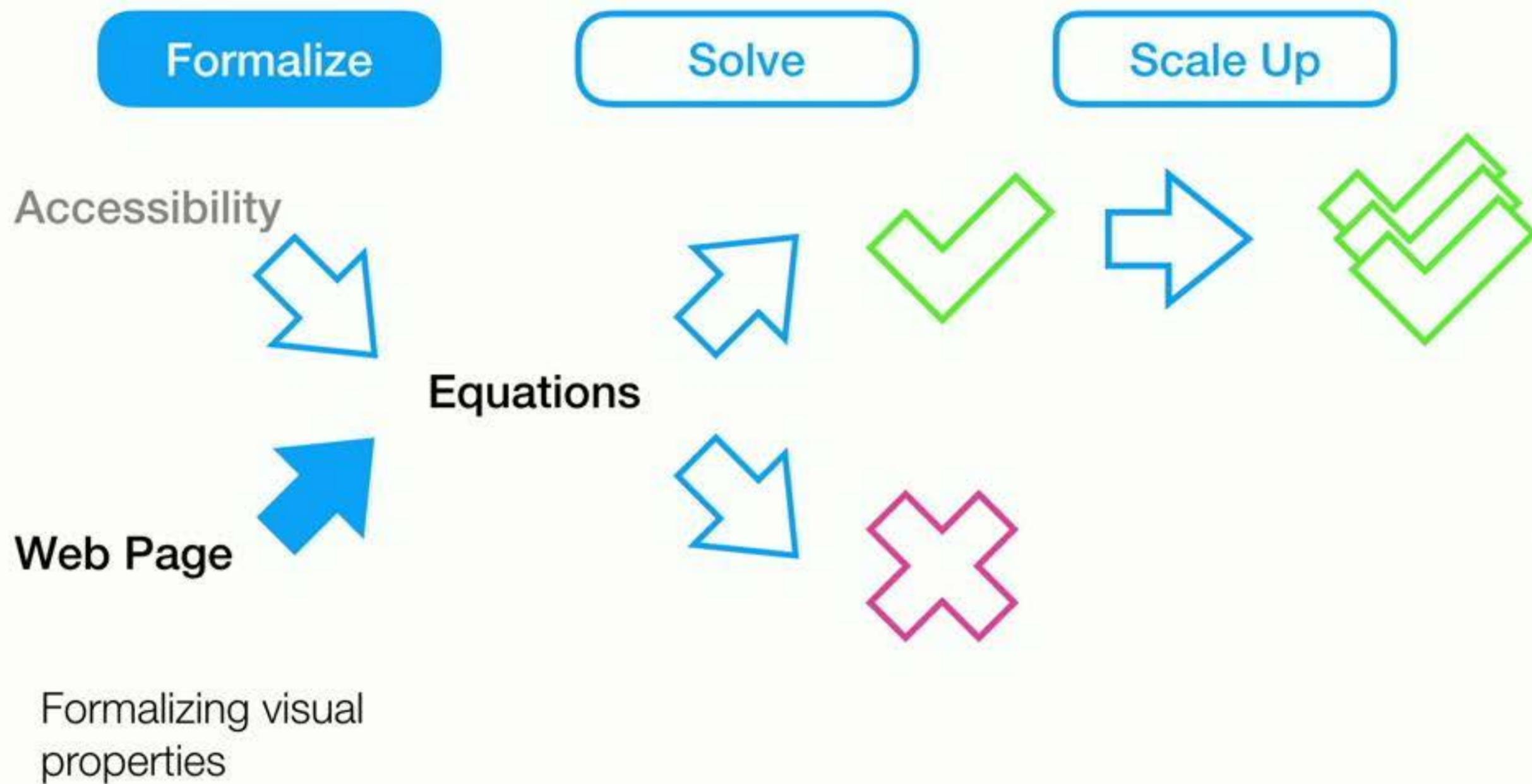


Pass thousands of conformance tests

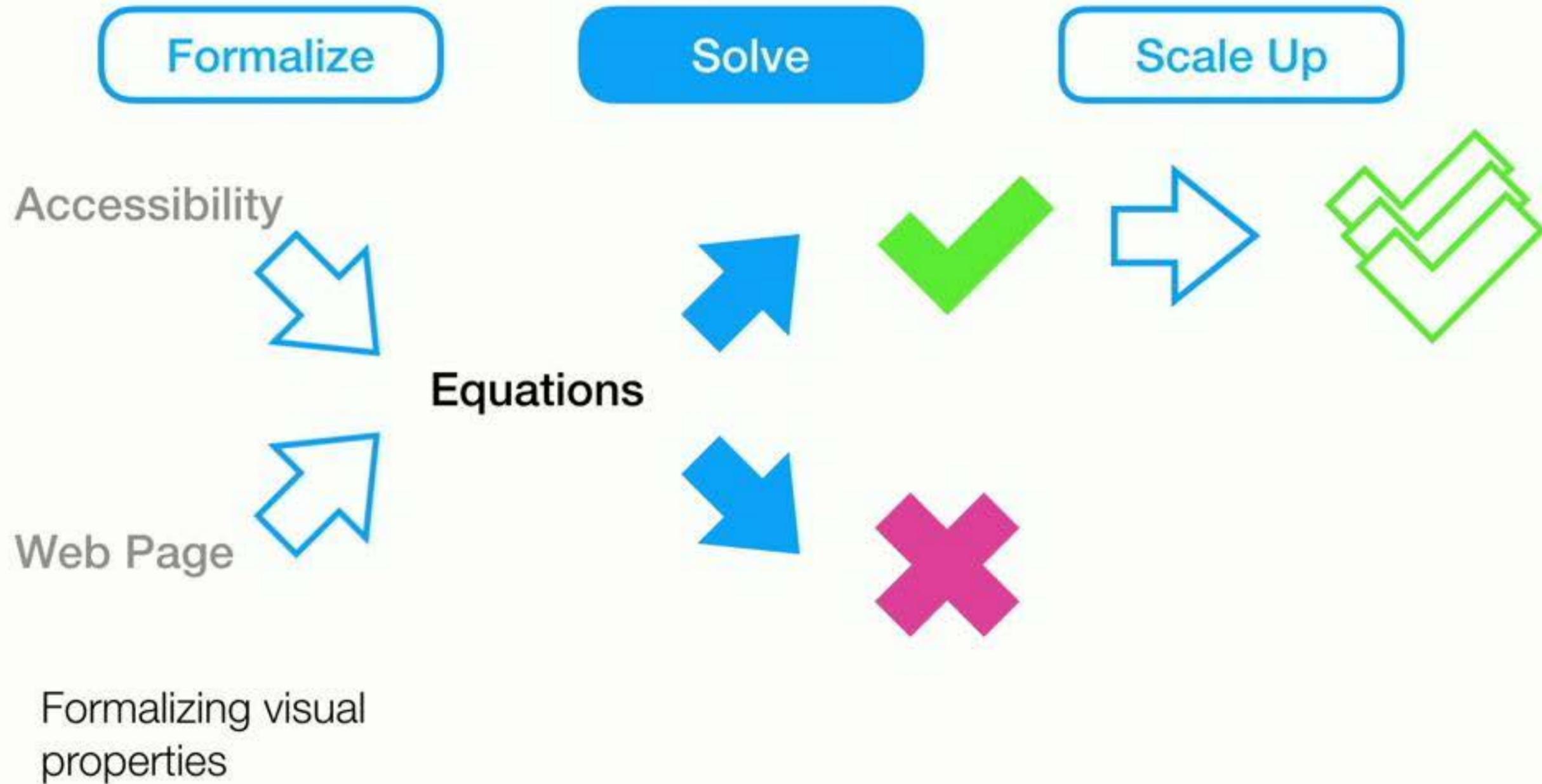
Found bugs in existing browsers

[OOPSLA'16]

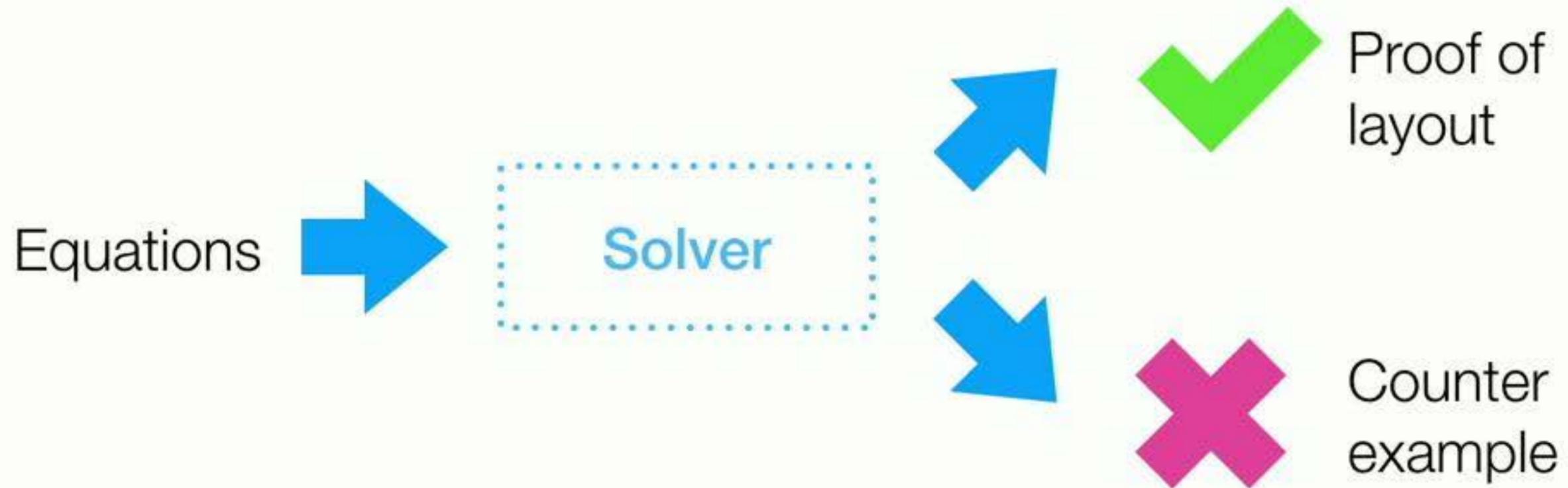
How VizAssert Works



How VizAssert Works



Solving the Equations



Solving the Equations



Solving the Equations



Quantifier **F**ree

Linear

Real **A**rithmetic

Solving the Equations



Quantifier **F**ree

Linear

Real **A**rithmetic \longrightarrow No rounding error

Solving the Equations



Quantifier **F**ree

Linear



No multiplication

Real **A**rithmetic



No rounding error

Solving the Equations



Quantifier **F**ree \longrightarrow No nested loops

Linear \longrightarrow No multiplication

Real **A**rithmetic \longrightarrow No rounding error

Solving the Equations



Simulated Rounding Error

$$a = b \longrightarrow -\varepsilon < a - b < \varepsilon$$

Real Arithmetic →

No nested loops

No multiplication

No rounding error

Solving the Equations



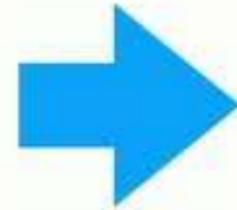
Quantifier **F**ree → No nested loops

Linear → No multiplication

Real **A**rithmetic → No rounding error ✓

Solving the Equations

Equations



QFLRA



Proof of layout



Counter example

Simplifying Multiplication

$a \times b$

No nested loops

No multiplication

Real Arithmetic



No rounding error



Solving the Equations



Quantifier **F**ree → No nested loops

Linear → No multiplication

Real **A**rithmetic → No rounding error



Solving the Equations



Bounded work per element

Only one loop: render each element

Quantifier **F**ree



No nested loops

Linear



No multiplication



Real **A**rithmetic



No rounding error



Solving the Equations



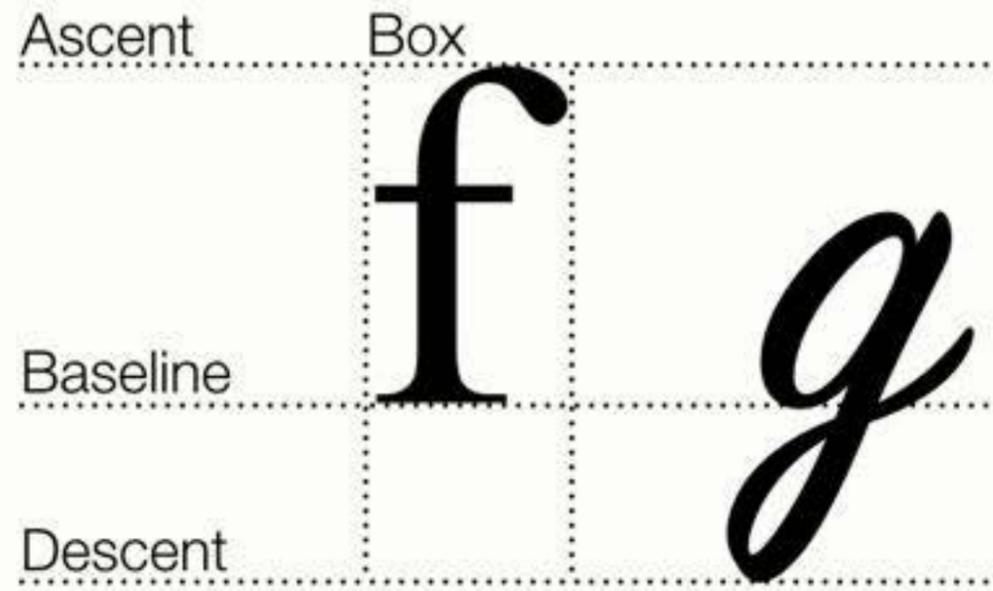
Problem: bounded work per element



Incrementalization, fusion, and unrolling

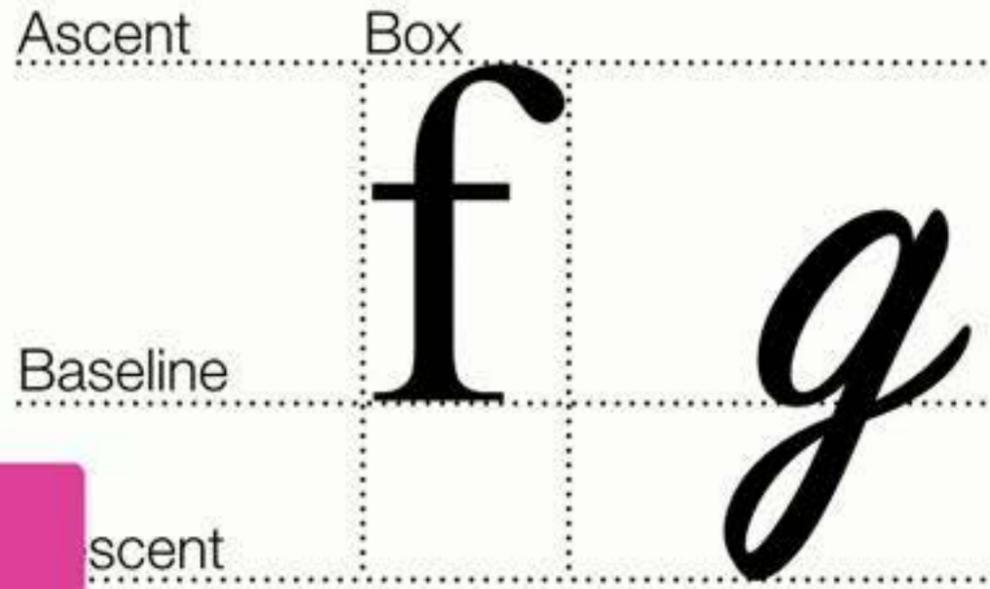
Inspired by compiler optimizations

Computing Line Height



“The line box height is the distance between the **uppermost** box top and the **lowermost** box bottom”

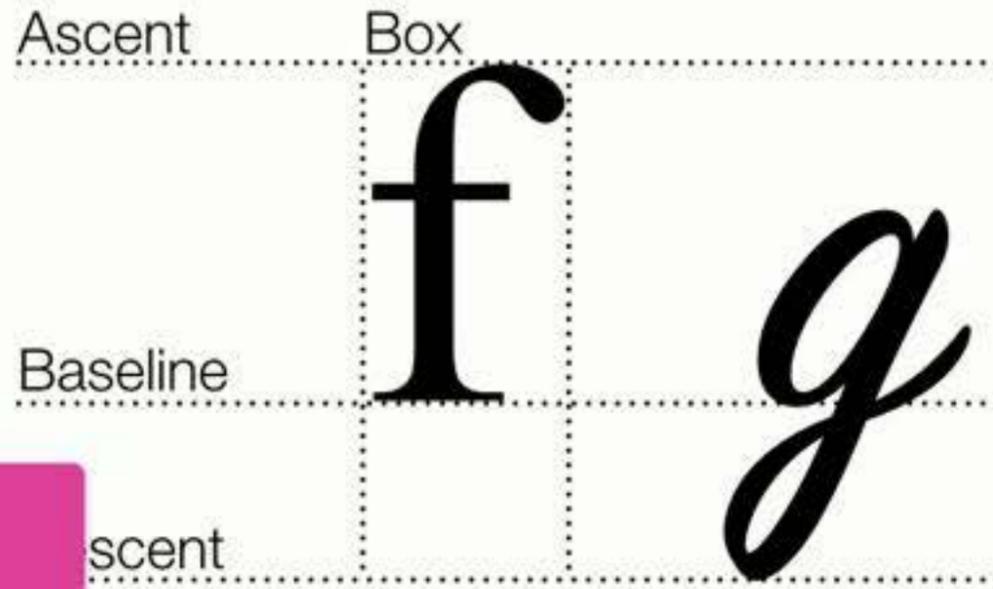
Computing Line Height



Loop over
elements in line

“The line box height is the distance between the **uppermost** box top and the **lowermost** box bottom”

Computing Line Height

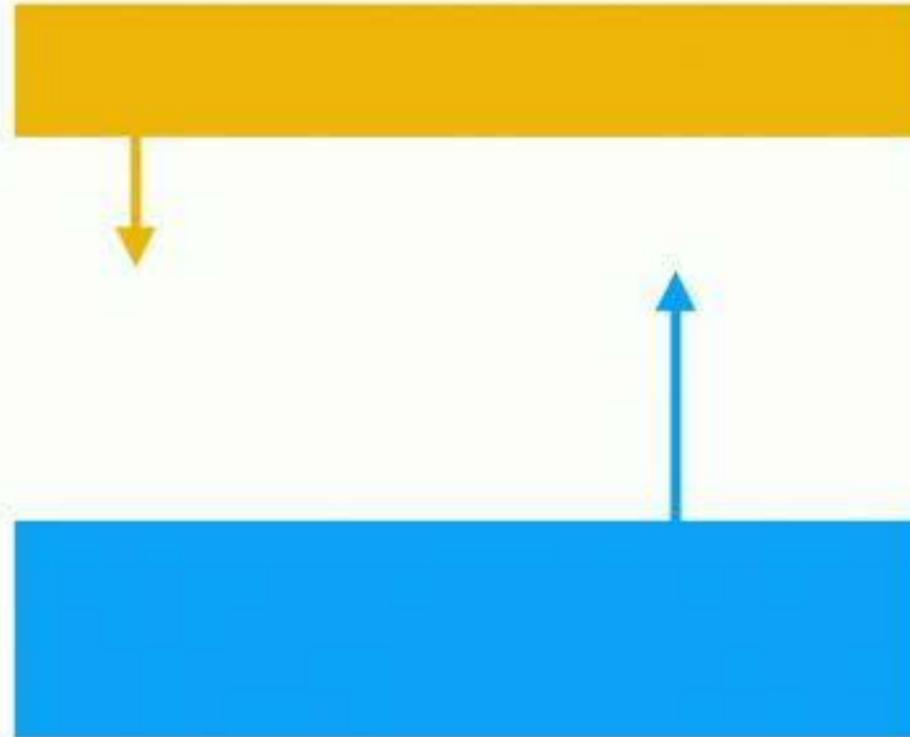


Loop over
elements in line

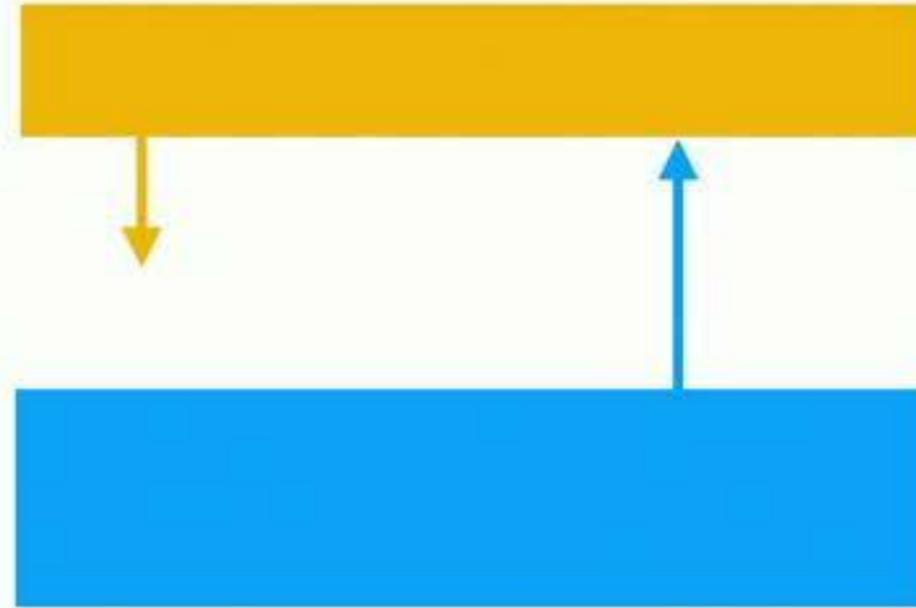
“The line box height is the distance between the **uppermost** box top and the **lowermost** box bottom”

Incrementalization: update running maximum

Computing Margins

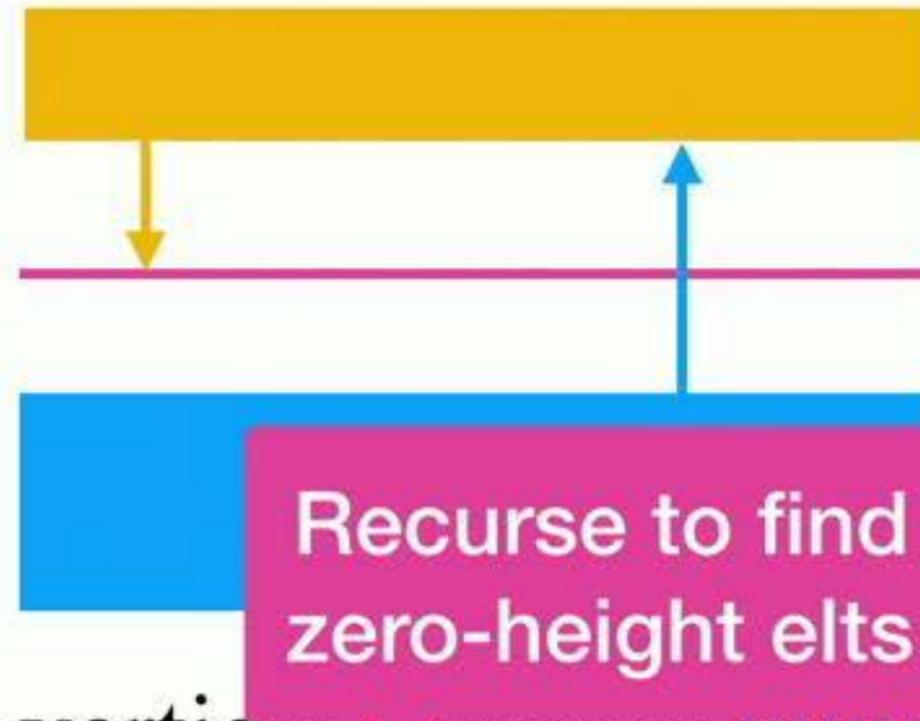


Computing Margins



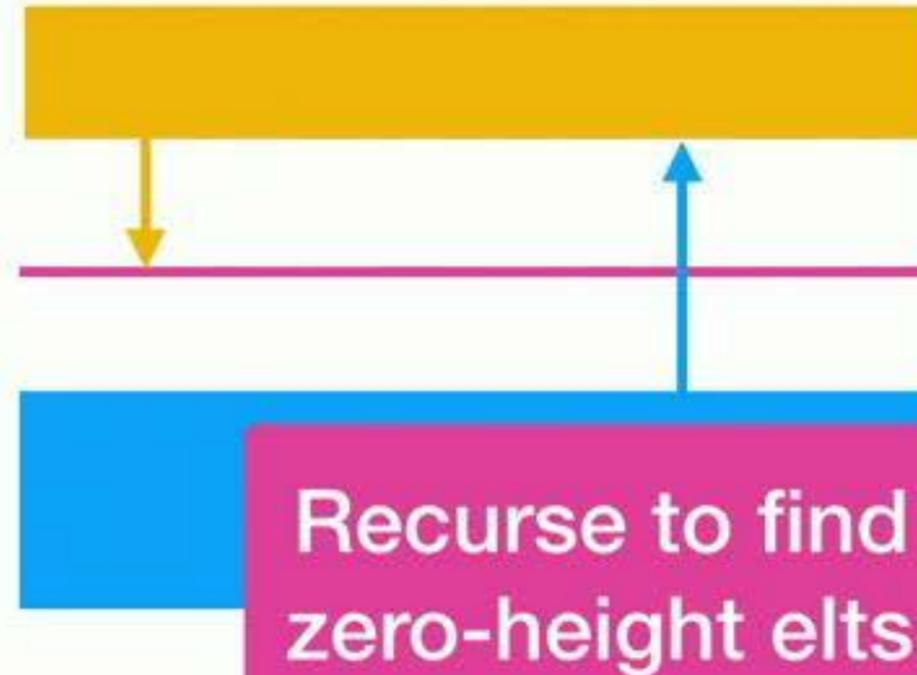
“Adjoining vertical margins **collapse**;
two margins are **adjoining** if and only if ...”

Computing Margins



“Adjoining vertical margins **collapse**;
two margins are **adjoining** if and only if ...”

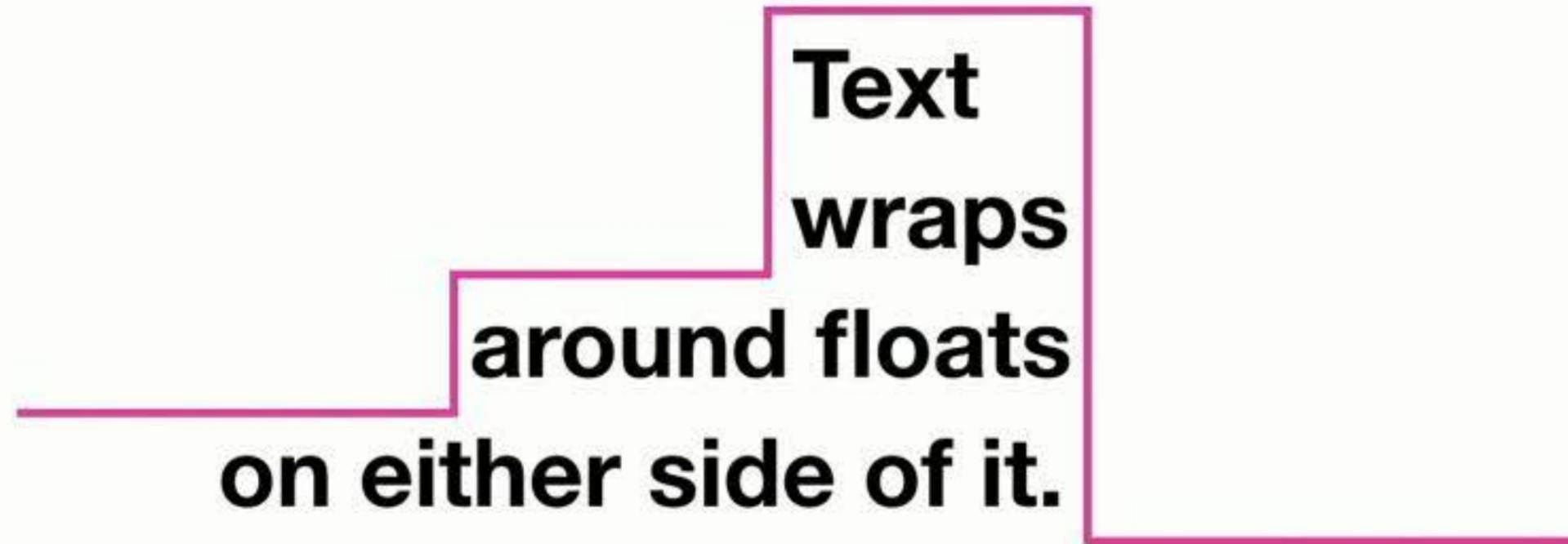
Computing Margins



“Adjoining vertical margins **collapse**;
two margins are **adjoining** if and only if ...”

Fusion: interleave with outer render loop

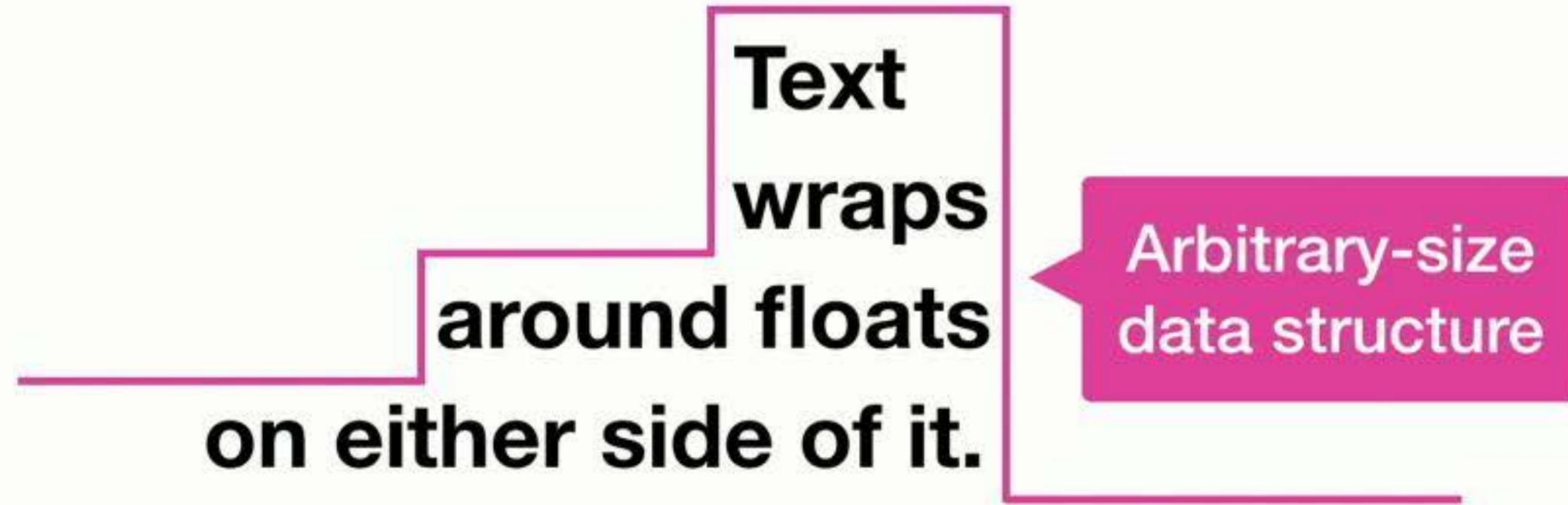
Computing Float Layout



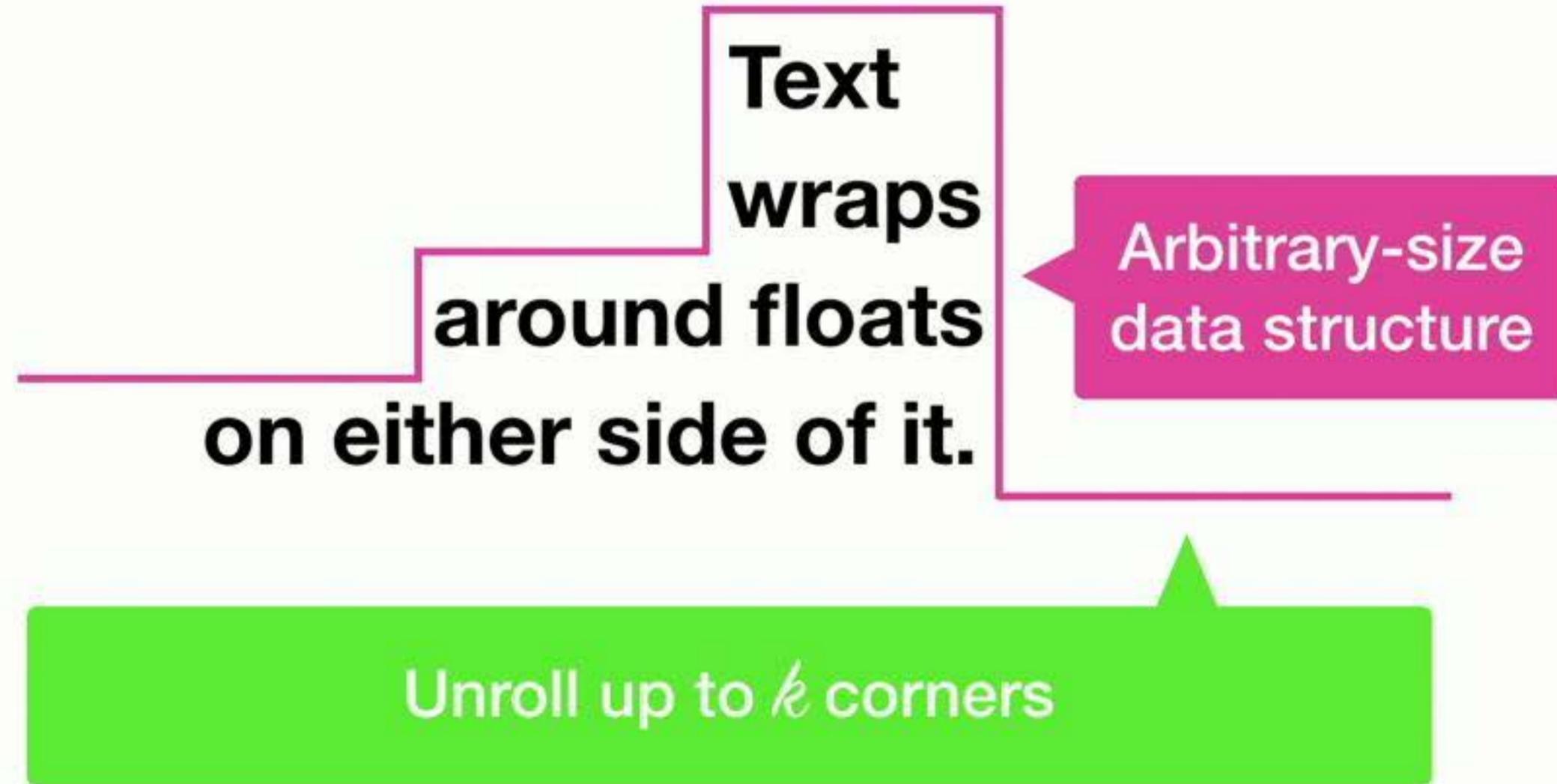
**Text
wraps
around floats
on either side of it.**

The diagram shows a pink stepped line representing a float. The text "Text wraps around floats on either side of it." is positioned to the right of the float, with the words "Text wraps" on the top step, "around floats" on the middle step, and "on either side of it." on the bottom step. This illustrates how text wraps around the float on both sides.

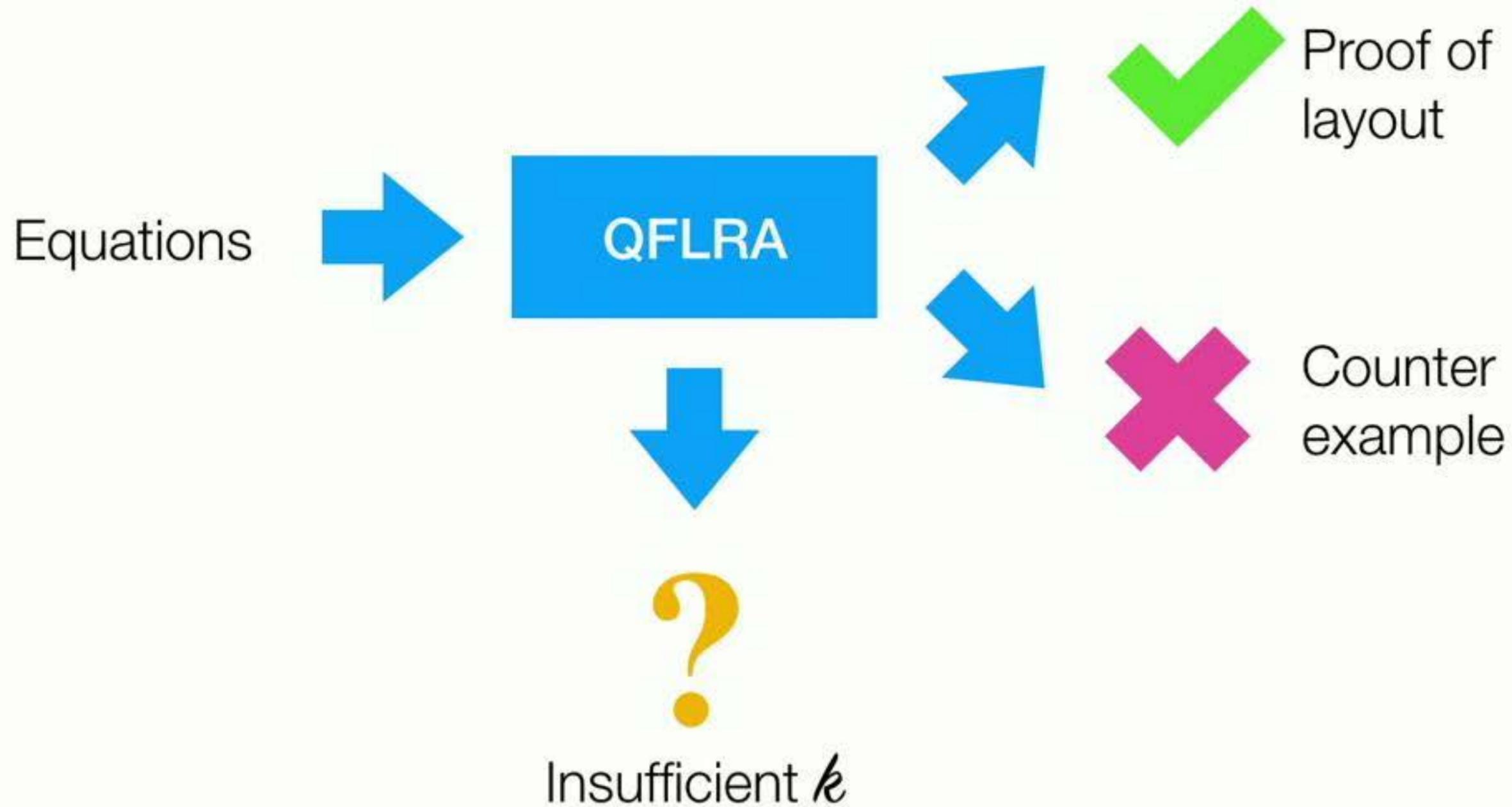
Computing Float Layout



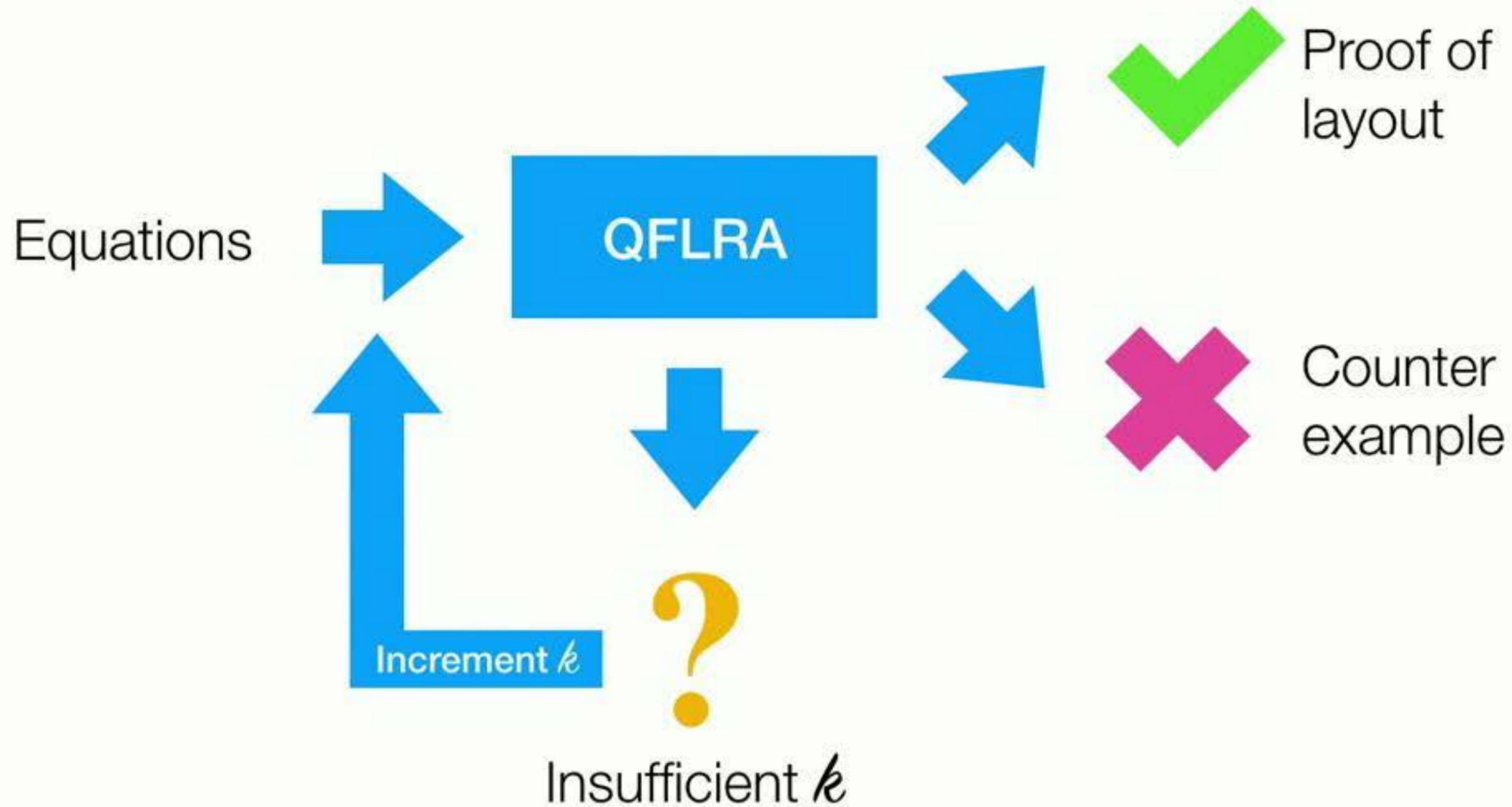
Computing Float Layout



Solving the Equations



Solving the Equations



Verifying Real Pages



Websites from design forum FreeWebsiteTemplates.com

Verifying Real Pages



Webs

Only use formalized subset of CSS

lates.com

62 web pages

Verifying Real Pages



Webs

Only use formalized subset of CSS

lates.com

62 web pages

14 properties

From Apple, Google, DOU accessibility guides

Verifying Real Pages



Webs

Only use formalized subset of CSS

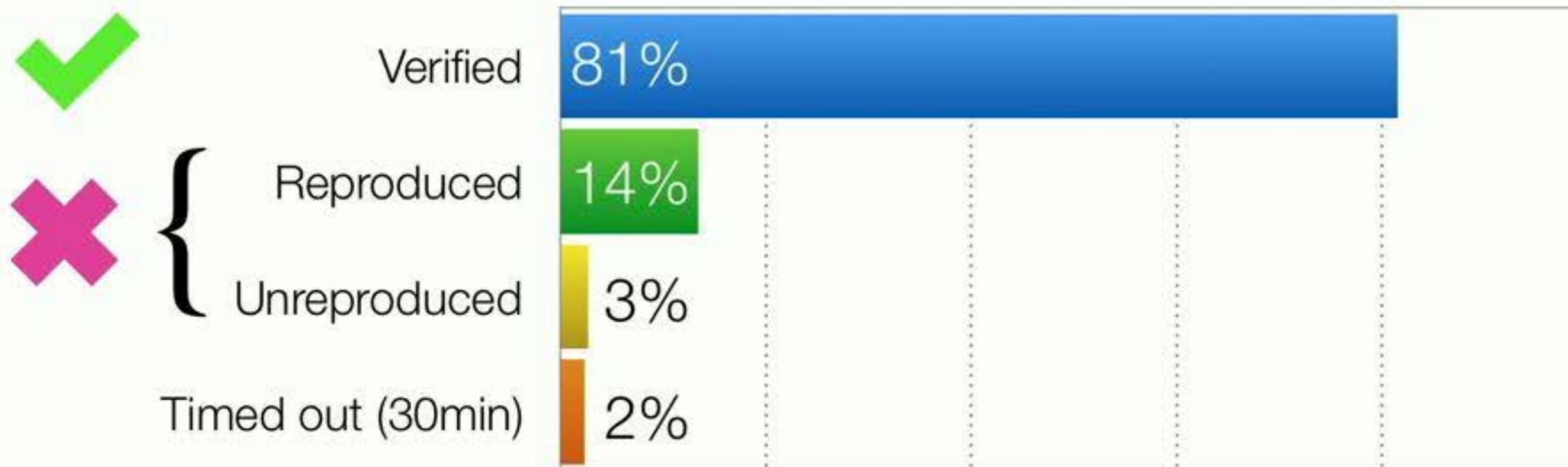
lates.com

62 web pages

14 properties

From Apple, Google, DOJ accessibility guides

Verifying Real Pages



Evaluate: verified majority of real-world inputs

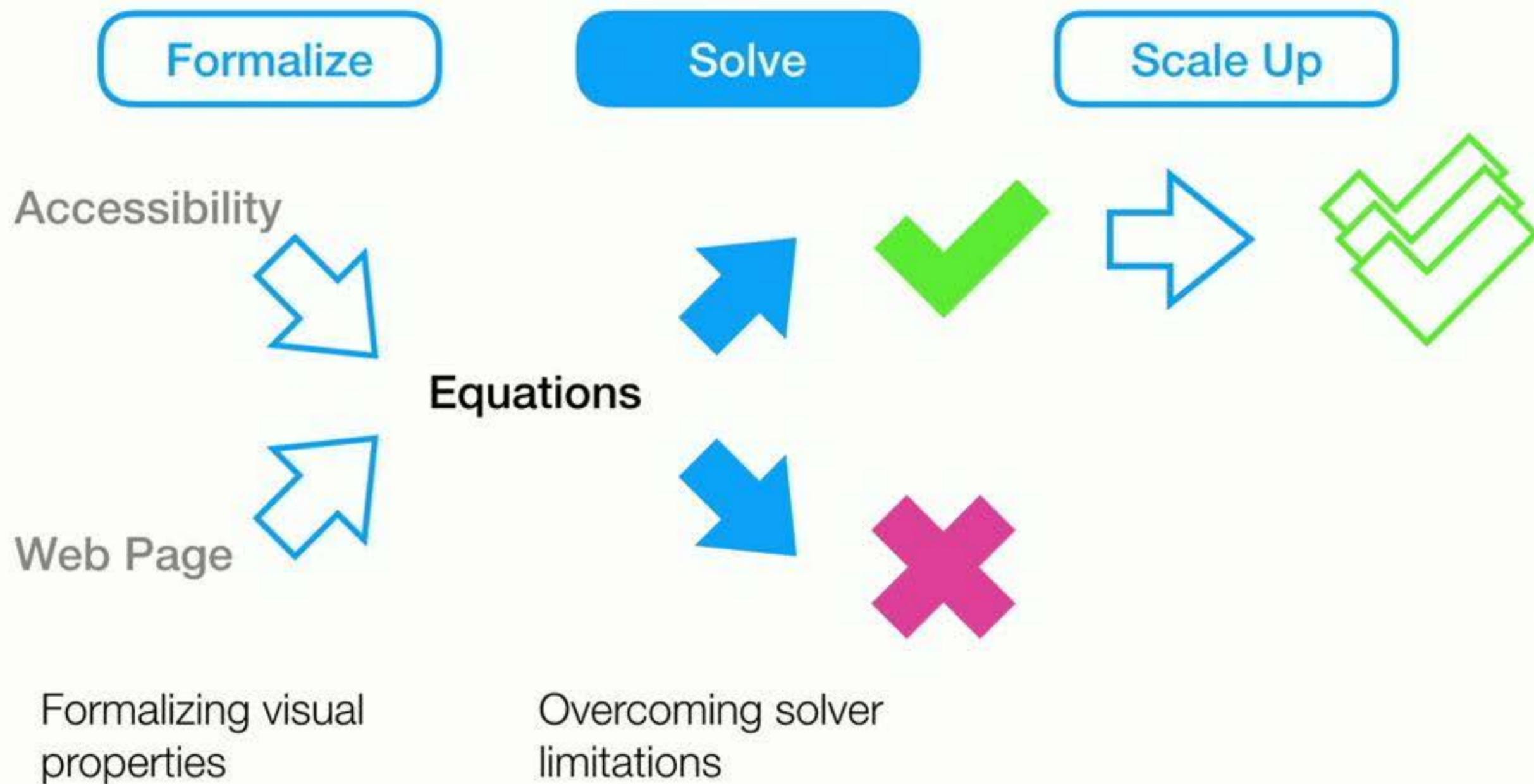


Found many real accessibility bugs

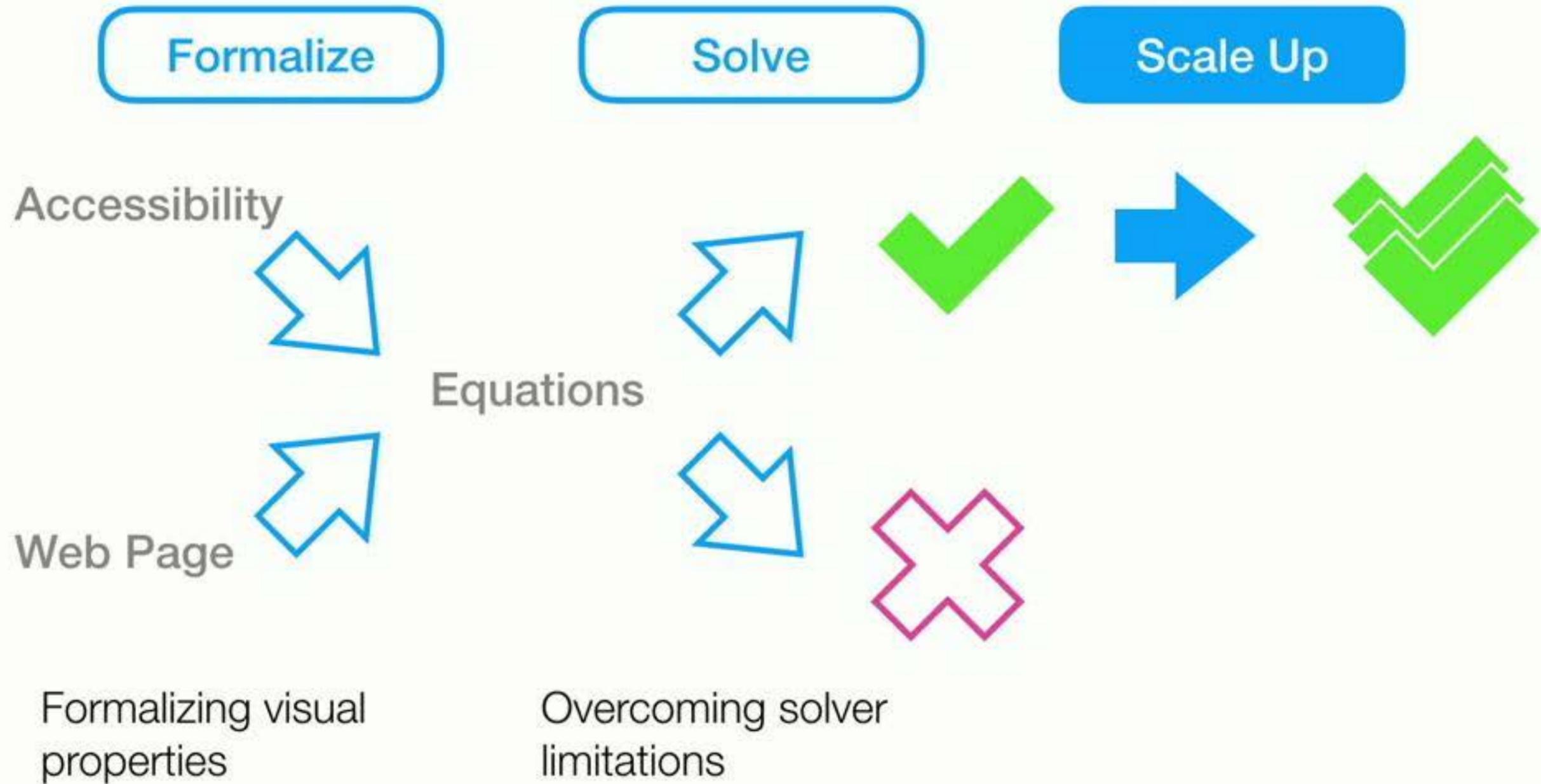
Few false positives and few timeouts

[PLDI'18]

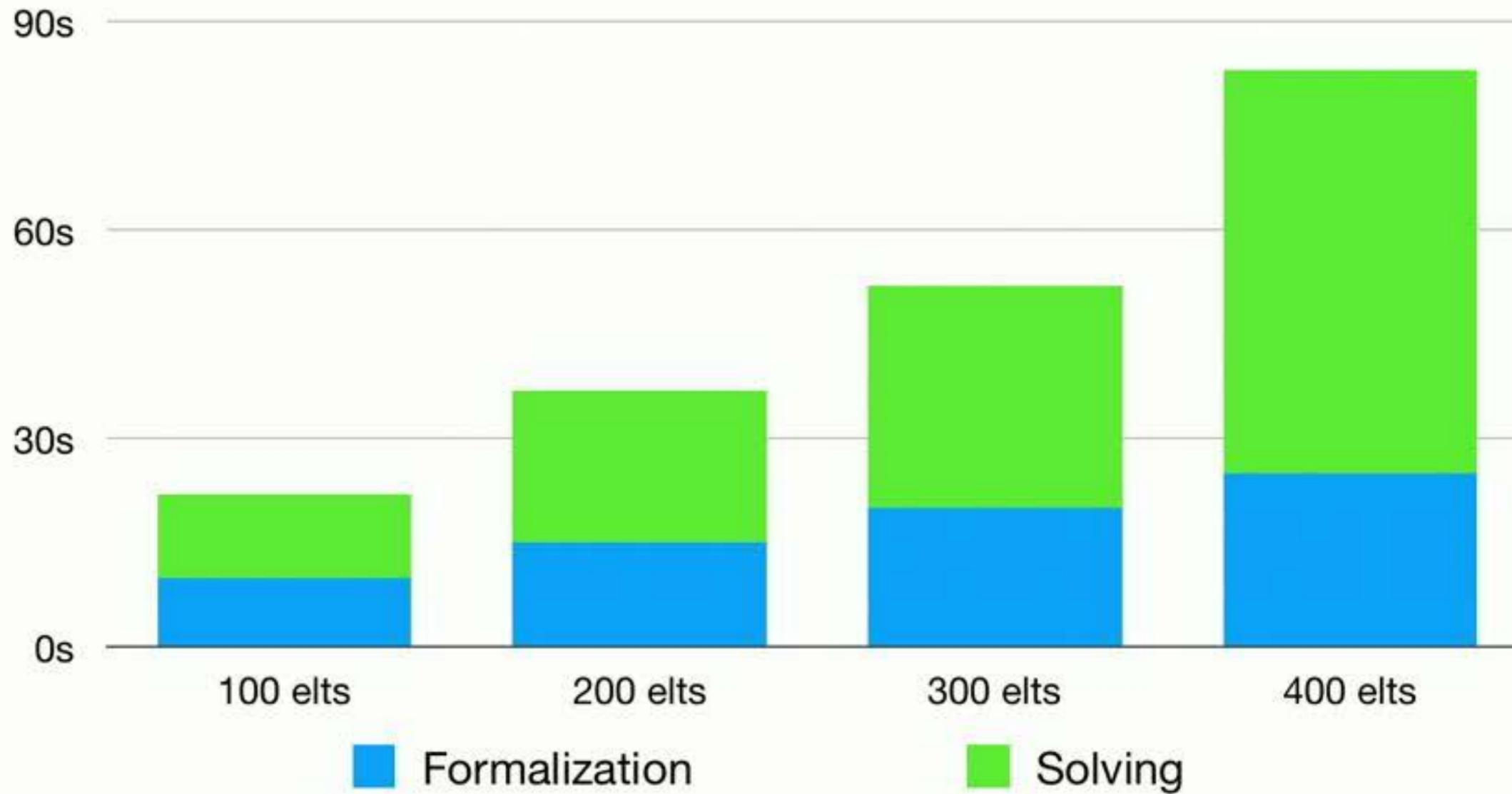
How VizAssert Works



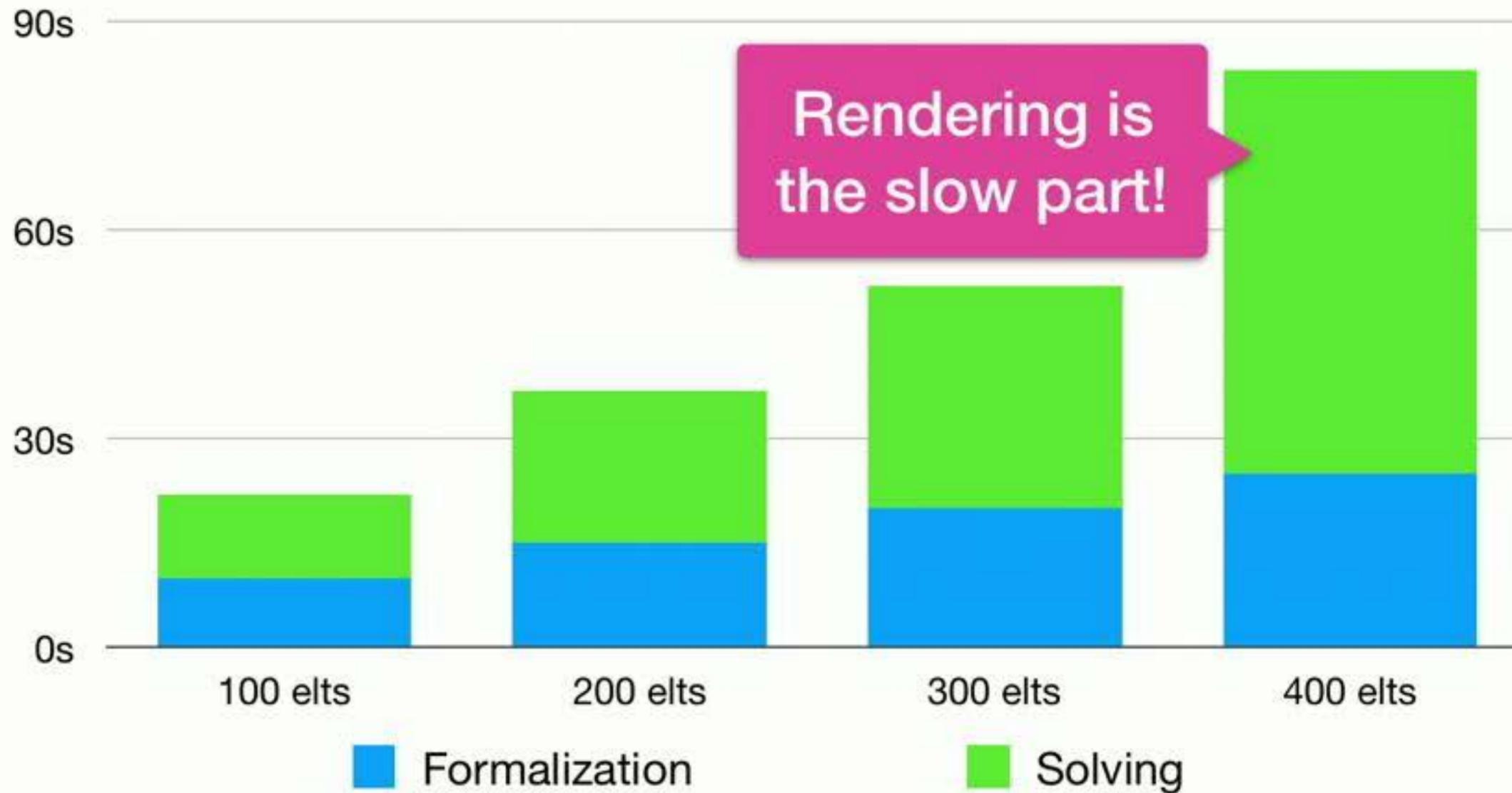
How VizAssert Works



Scaling Verification



Scaling Verification

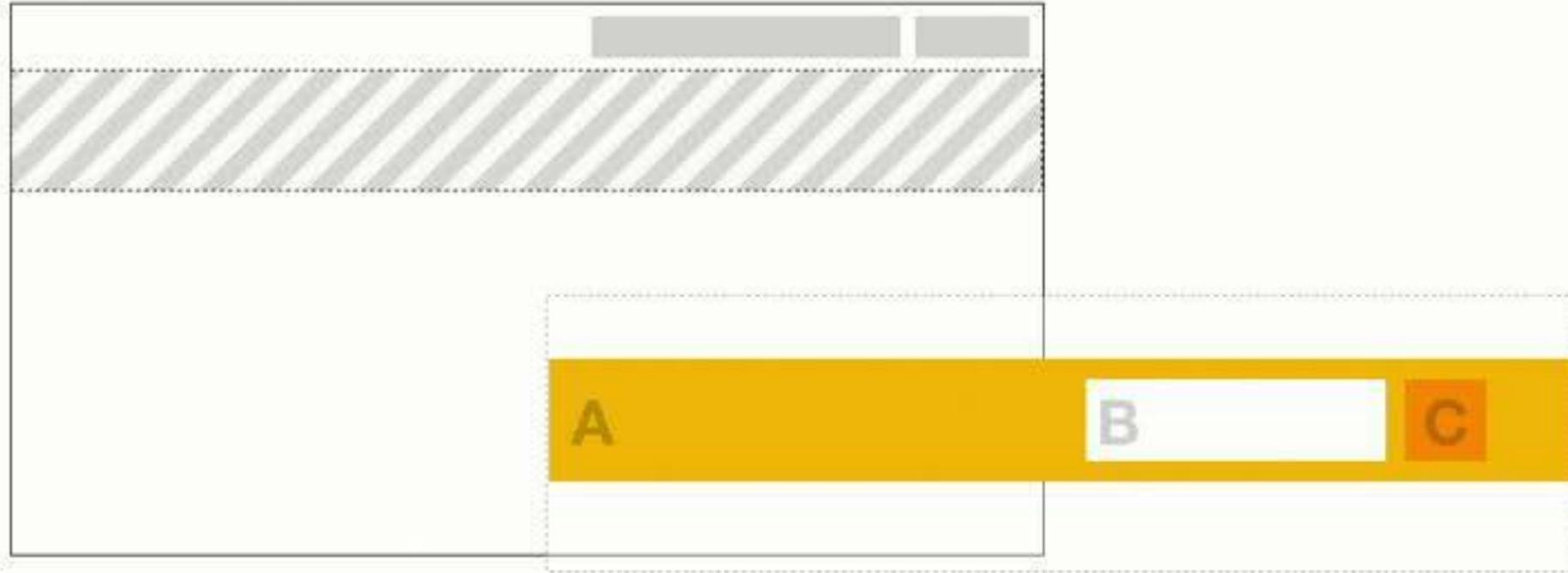


Scaling Verification



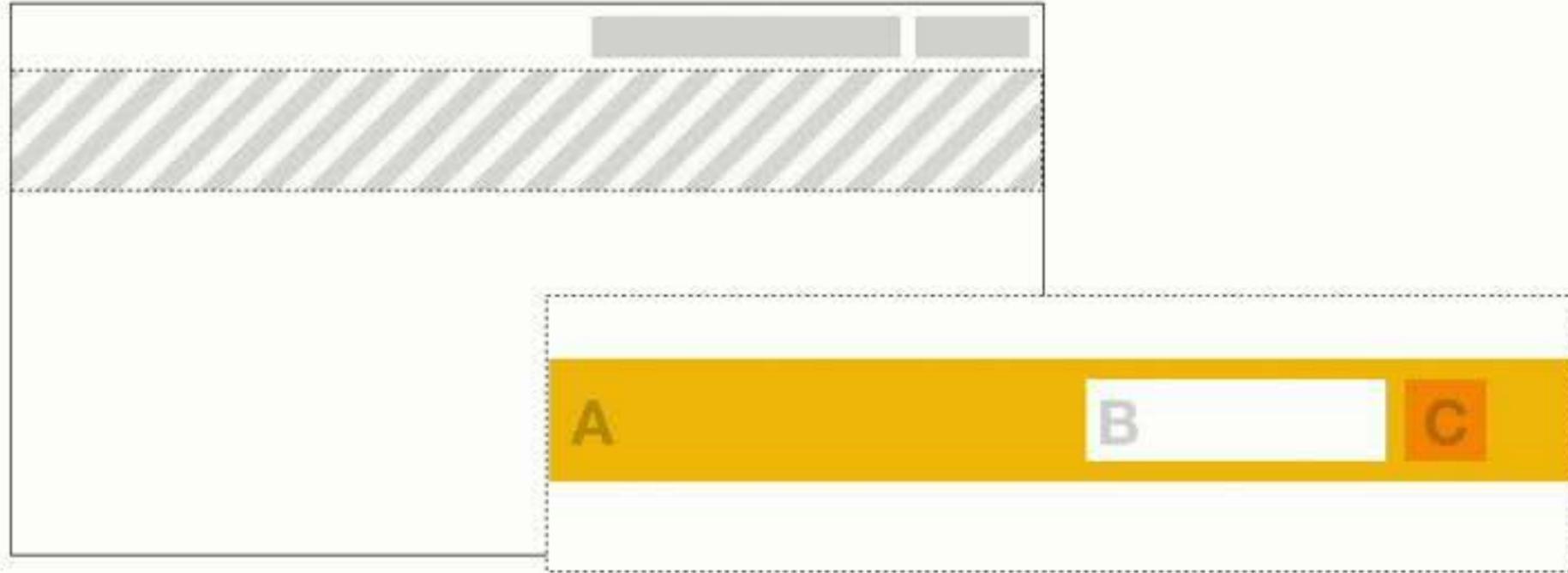
Problem: reason about large pages quickly

Scaling Verification



Problem: reason about large pages quickly

Scaling Verification



Problem: reason about large pages quickly



Divide web page into small components

Combine components with rely/guarantee logic

Isolating Components

Template

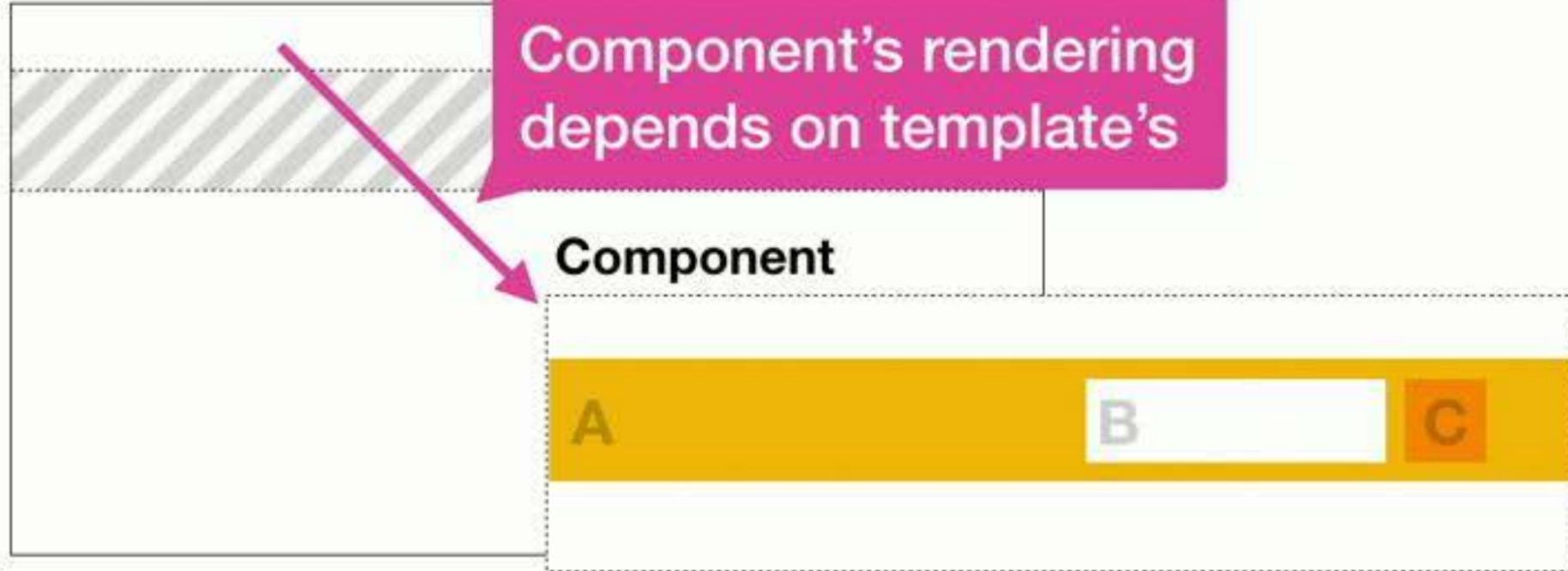


Component



Isolating Components

Template



Component's rendering depends on template's

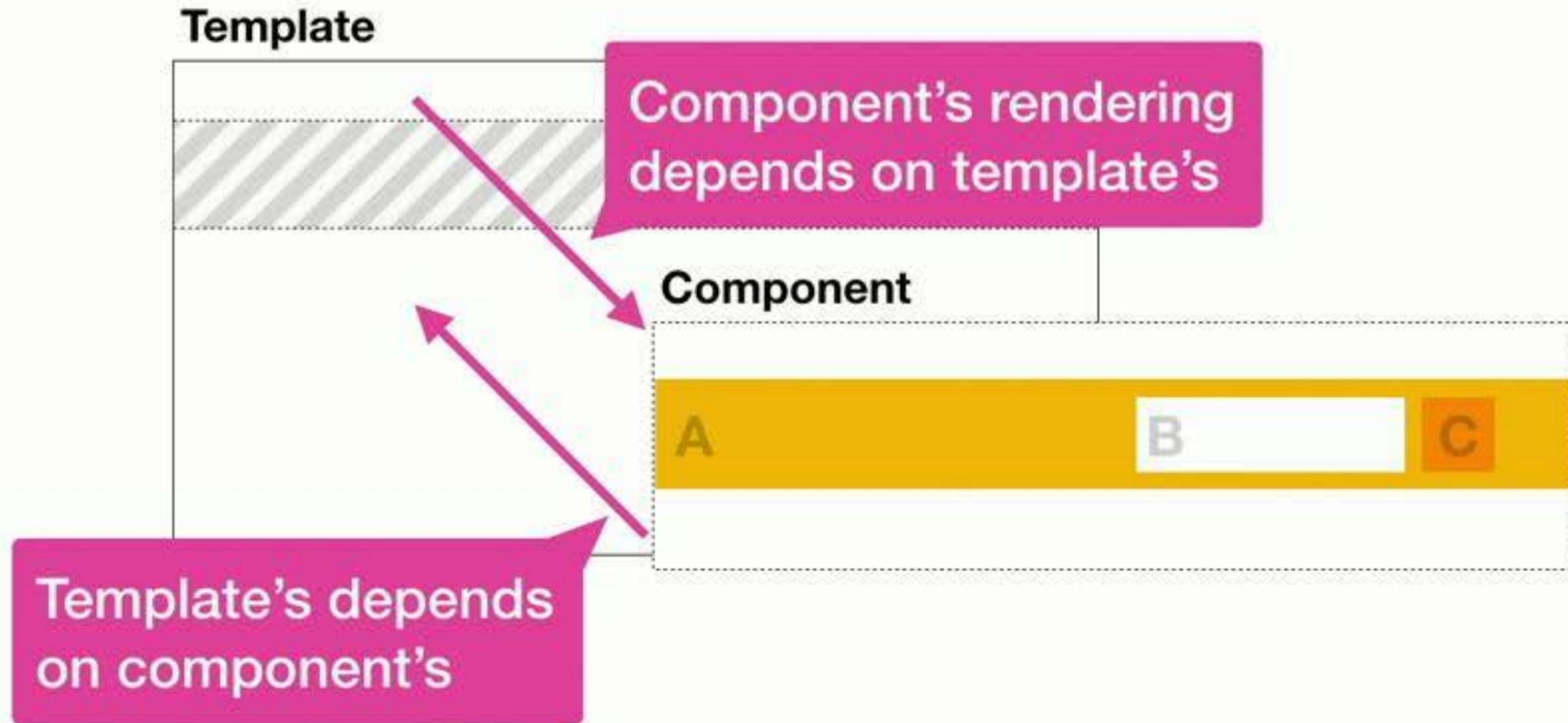
Component

A

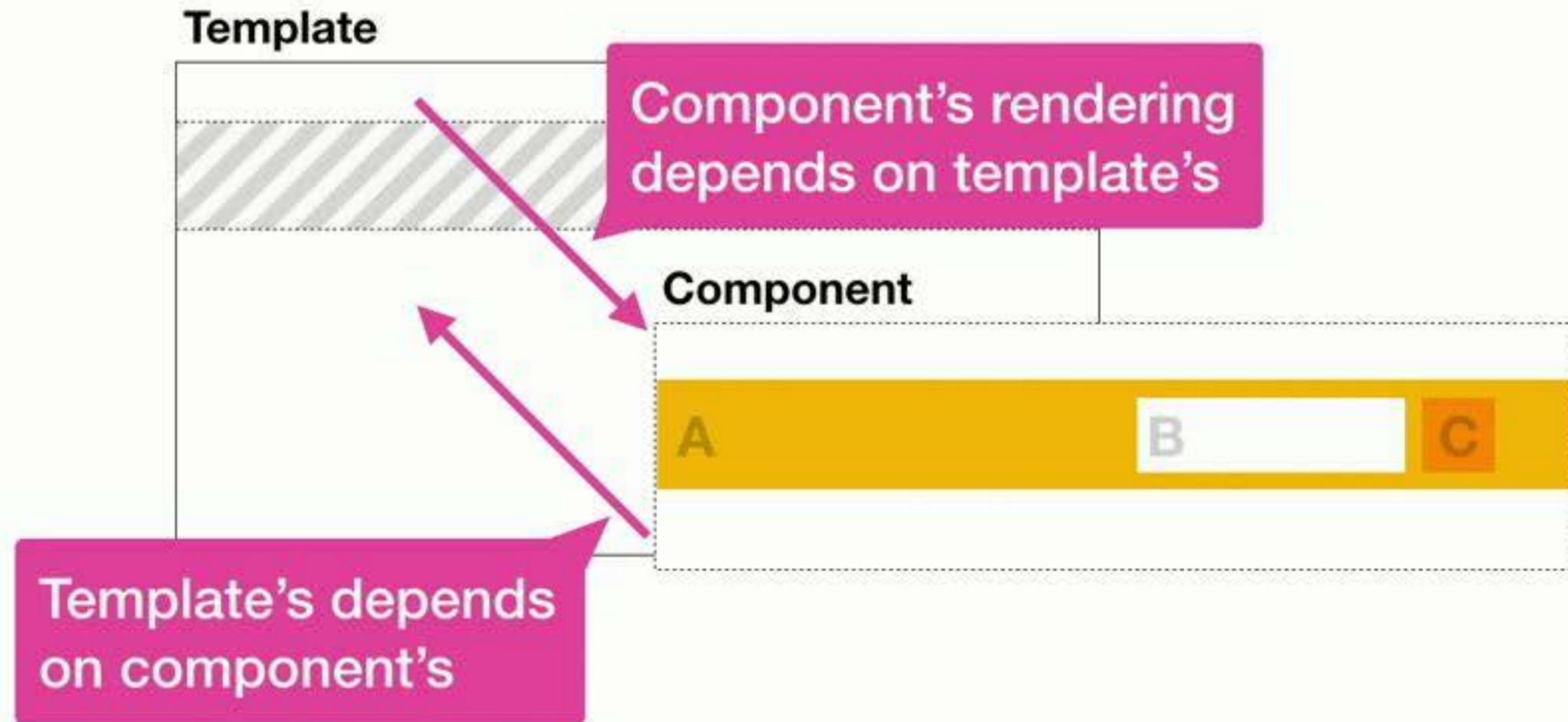
B

C

Isolating Components



Isolating Components



No module or function boundaries!

Isolating Components

?

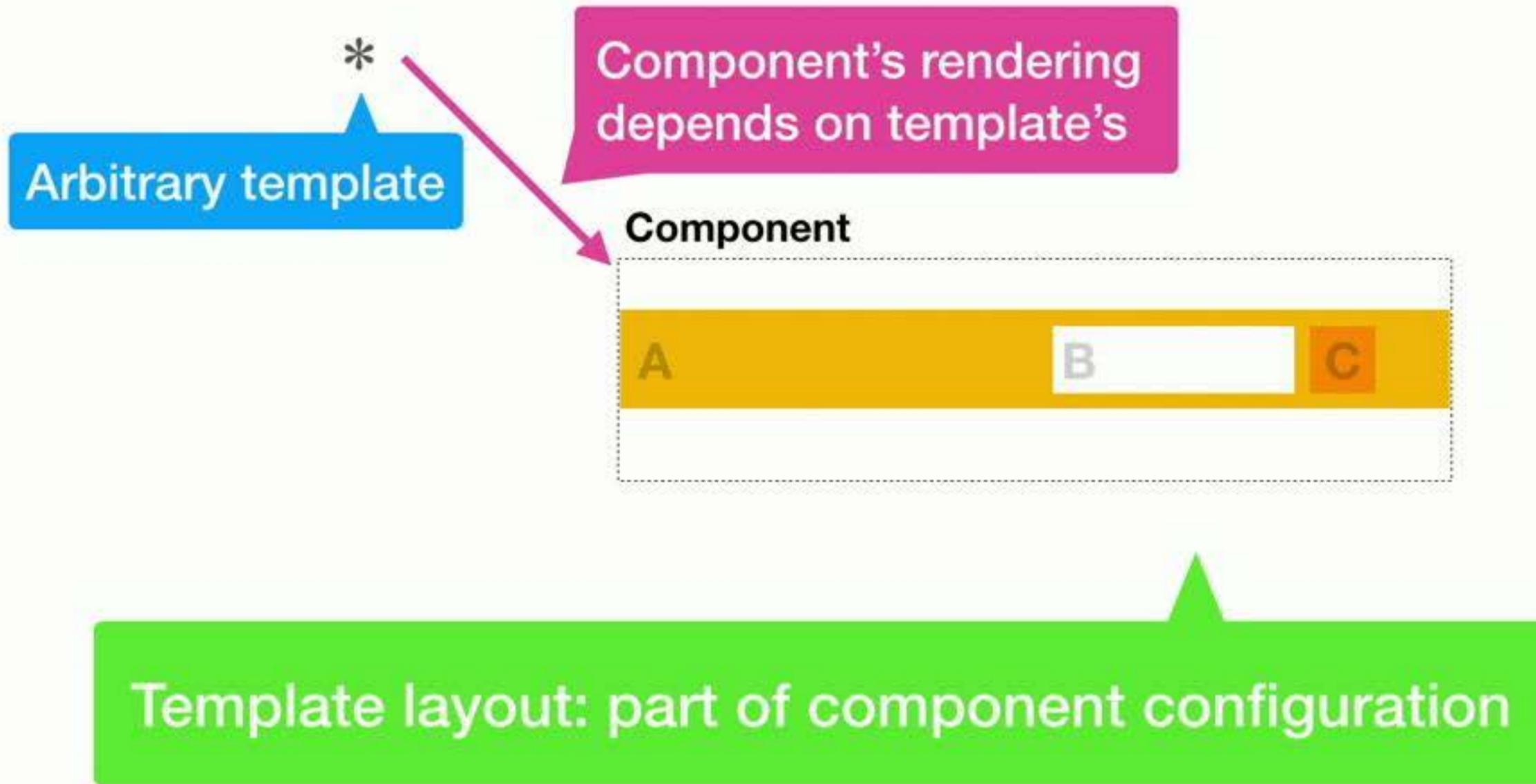
Component's rendering depends on template's

Component



No module or function boundaries!

Isolating Components



Isolating Components

Precondition

Width available
Current font size
Floating elements

Component's rendering depends on template's

Component



Template layout: part of component configuration

Rely / Guarantee

Component

Precondition \Rightarrow Specification

Rely / Guarantee

Precondition

Precondition \Rightarrow Specification

Rely / Guarantee

Precondition

Precondition \Rightarrow Specification

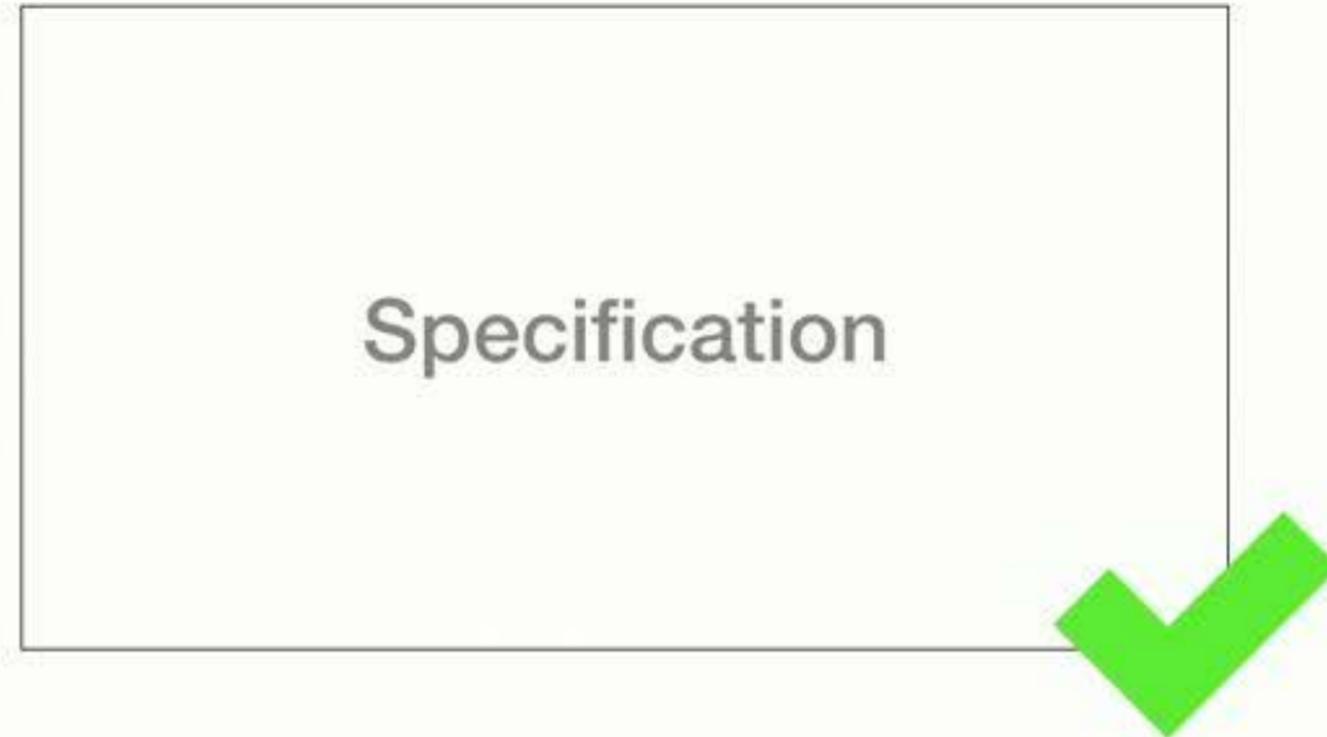
Rely / Guarantee

Precondition

&&

Precondition \Rightarrow Specification

Rely / Guarantee

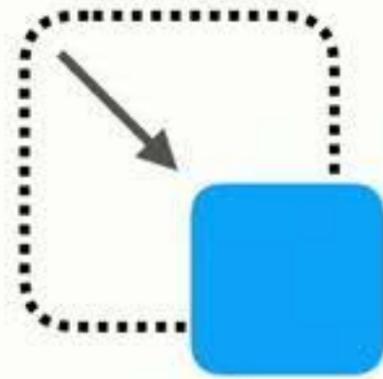


Preconditions checked purely logically

No rendering \Rightarrow fast

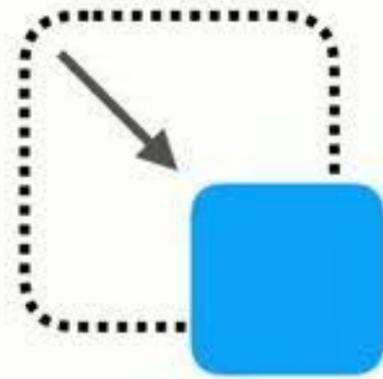
Improving Scale

Problem Size



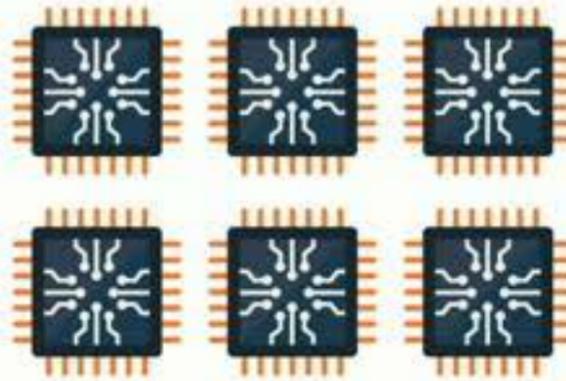
Improving Scale

Problem Size



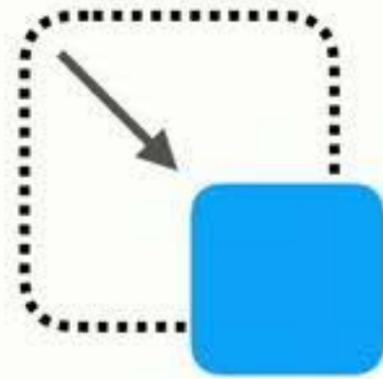
+

Parallelism



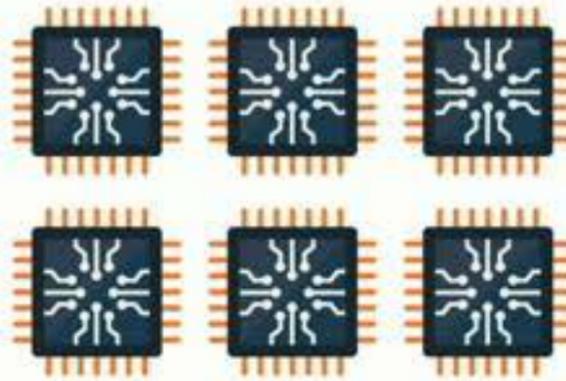
Improving Scale

Problem Size



+

Parallelism



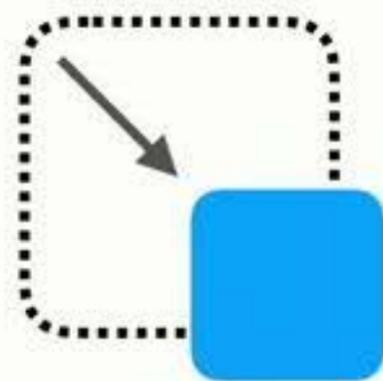
+

Caching



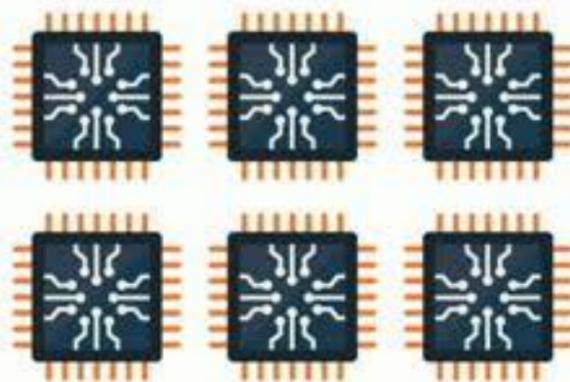
Improving Scale

Problem Size



+

Parallelism



+

Caching



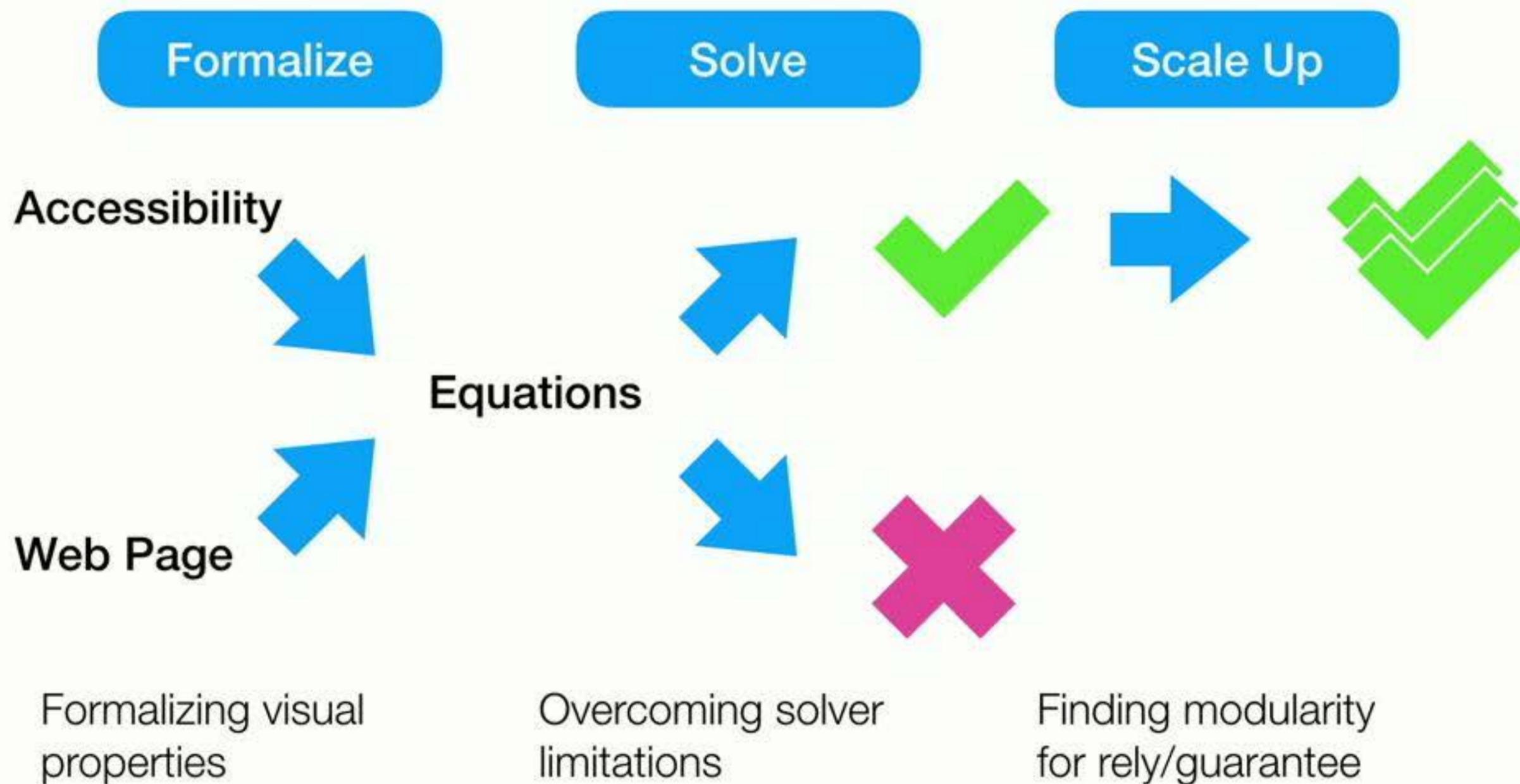
Evaluate: broader class of verified pages



Scaled to 11× larger pages, to 1400× faster

Scaled to multiple pages on one site

How VizAssert Works



Future Work

Frontend code (JavaScript)

Backend code (Python, PHP, ...)

Other platforms (Android, iOS...)

User studies with designers

Future Work

Frontend code (JavaScript)

Backend code (Python, PHP, ...)

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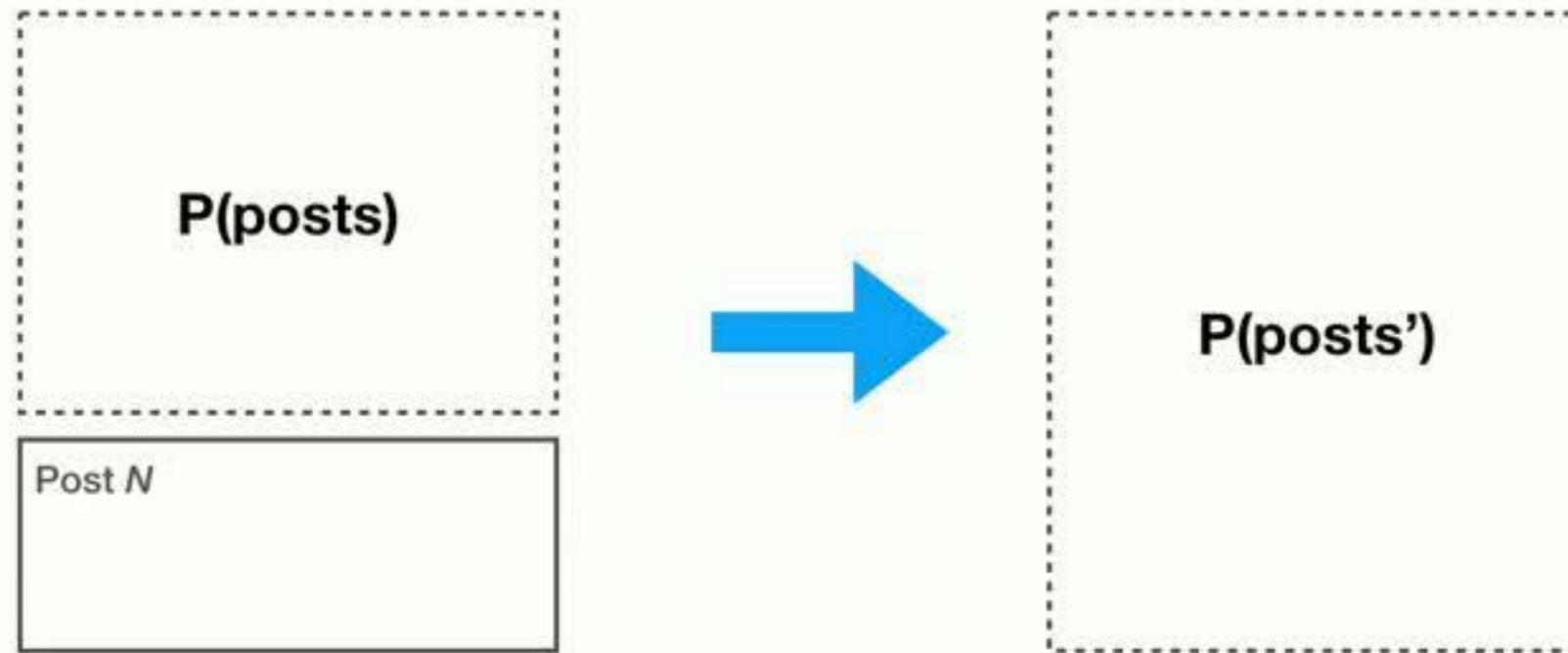
User studies with designers

Dynamic Web Pages



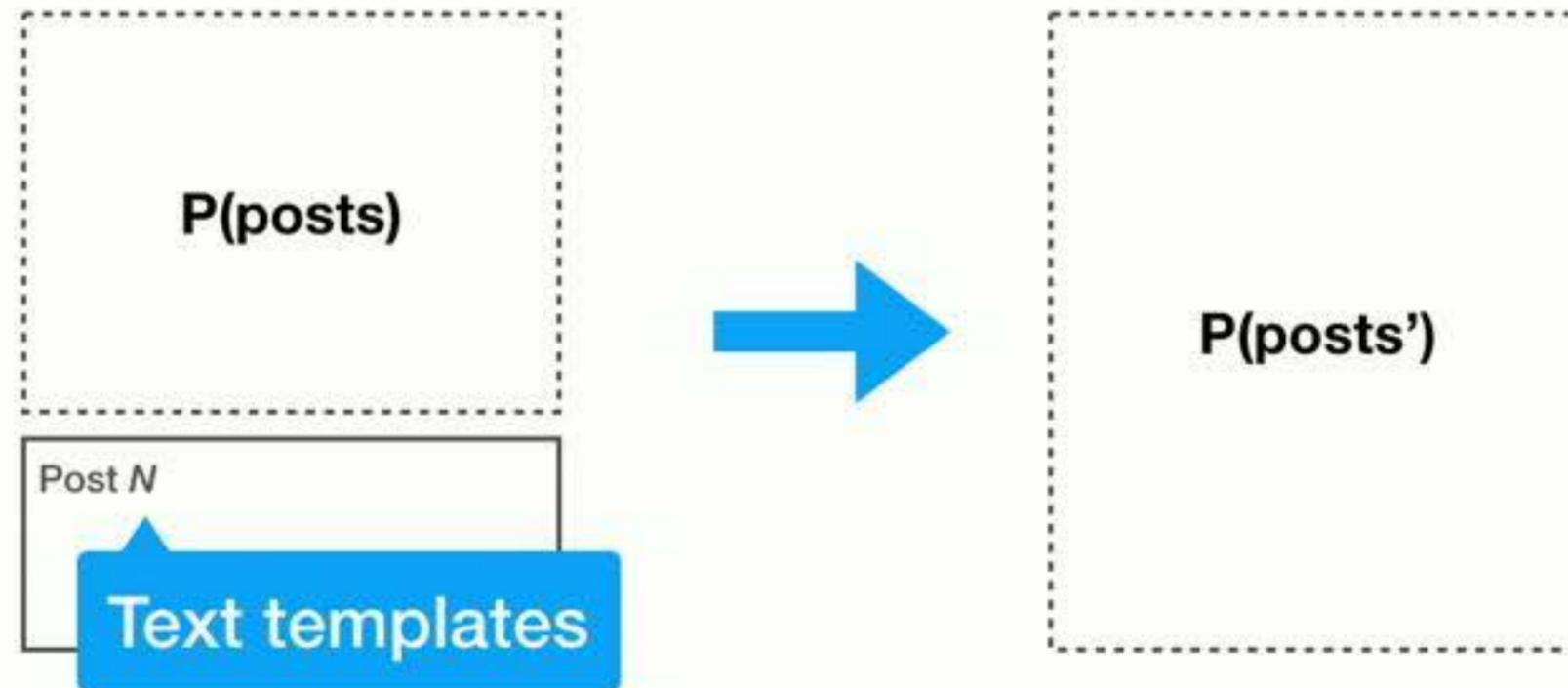
How can we verify pages if we don't know their contents?

Dynamic Web Pages



Induction over structure of the page

Dynamic Web Pages



Induction over structure of the page

Future Work

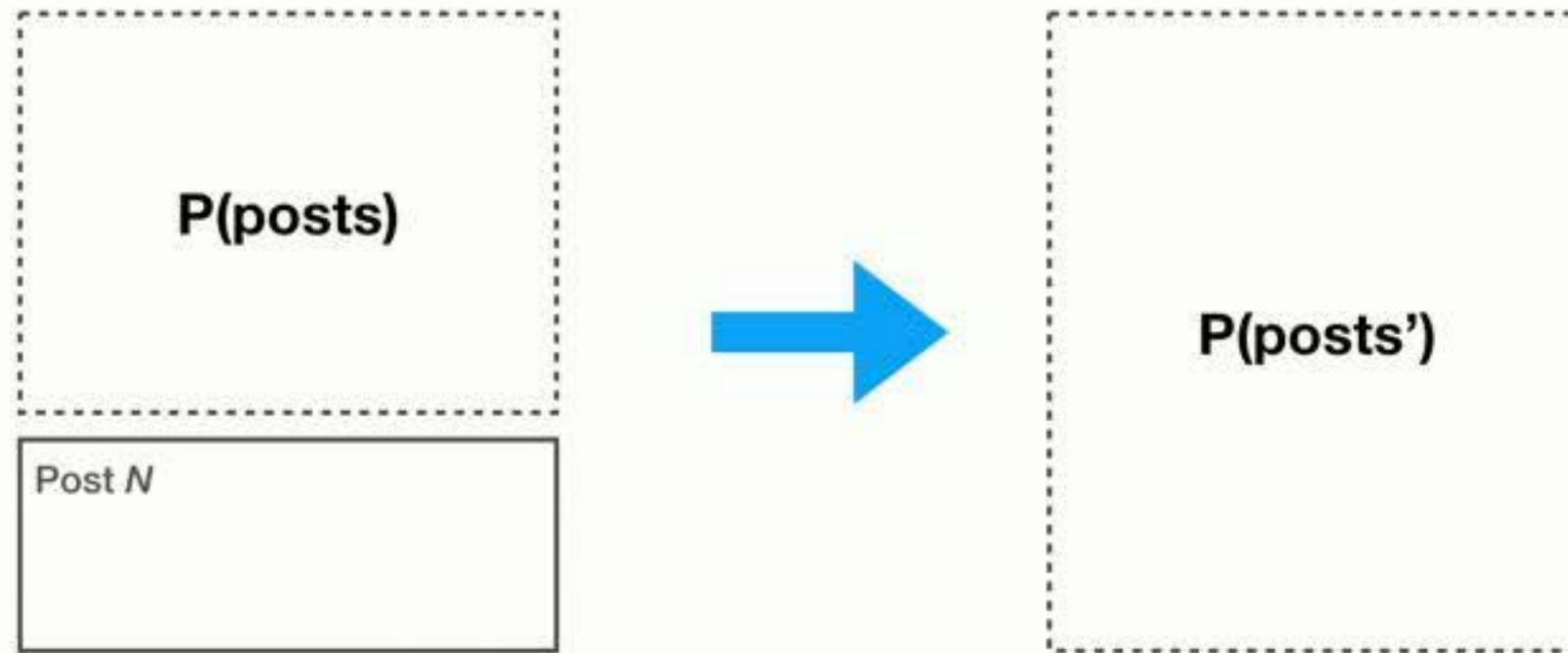
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Dynamic Web Pages



Induction over structure of the page

Future Work

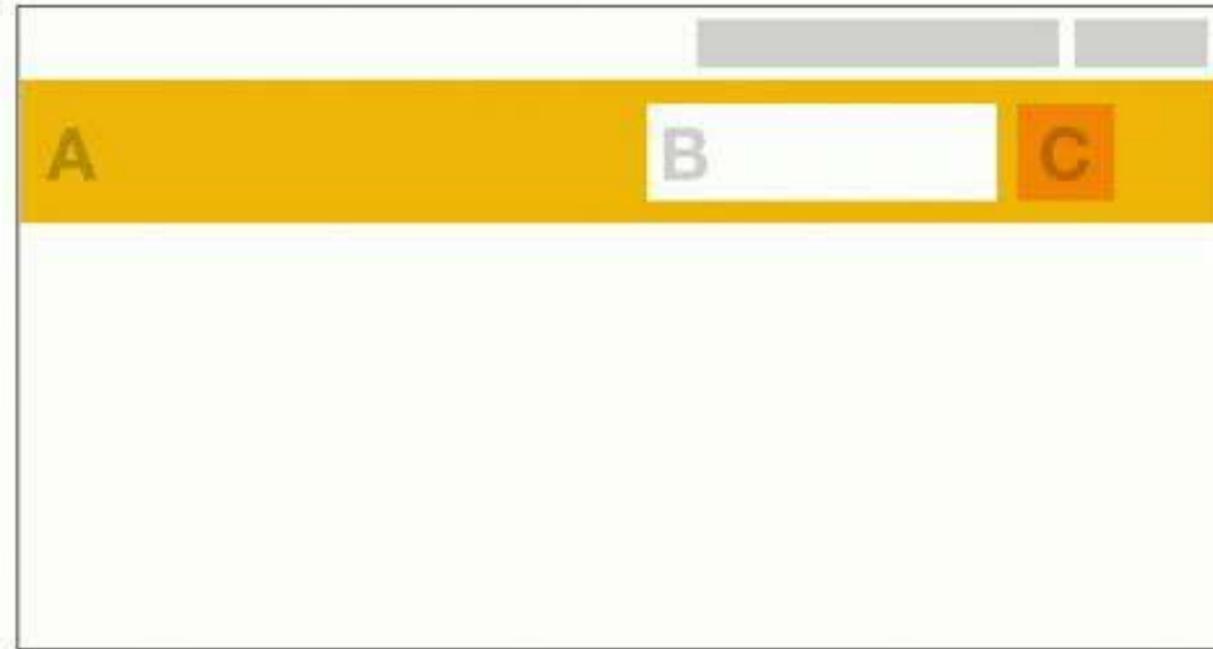
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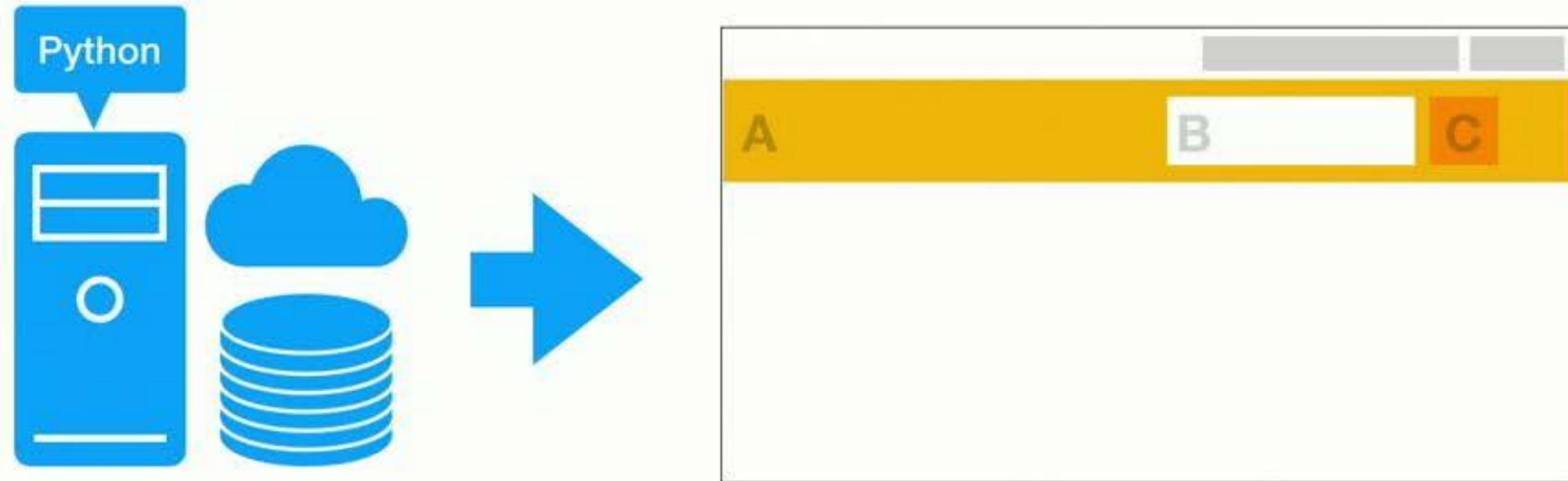
Other platforms (Android, iOS...)

User studies with designers

Web Page Backends



Web Page Backends



Web Page Backends

```
<div id='header'><h1>A</h1><form>...
```

```
<li class='search-result'>  
  <h2>  
    <a href="{obj.url}">{obj.name}</a>  
  </h2>  
  <p>{obj.description}</p>  
</li>
```

Web Page Backends

```
write(" <div id='header'><h1>A</h1><form>... ")
```

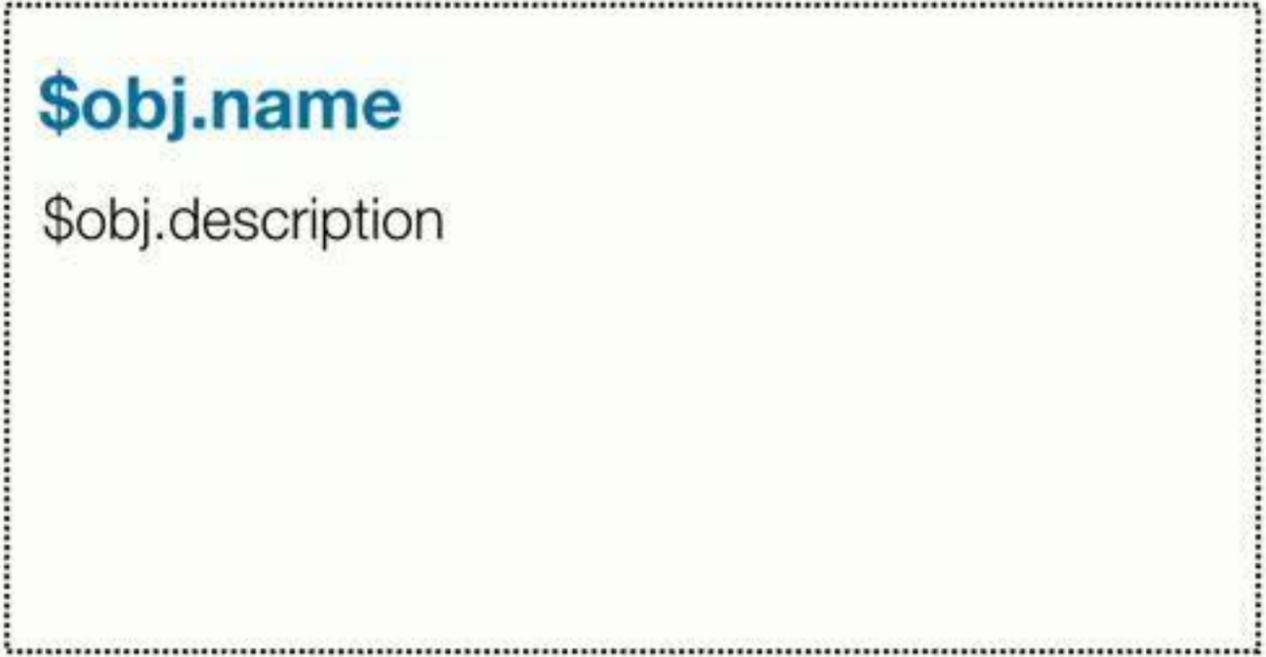
for obj in results:

```
write(" <li class='search-result'>  
    <h2>  
        <a href="{obj.url}">{obj.name}</a>  
    </h2>  
    <p>{obj.description}</p>  
</li> ")
```

Web Page Backends

```
write(  )
```

for obj in results:

```
write(  )
```

Web Page Backends

```
write(toolbar.height > 10)
```

for obj in results:

```
write($obj.name &&  
$obj.description && result.height > 0)
```

Web Page Backends

```
write( toolbar.height > 10 )
```

for obj in results:

```
write( result.y > 10 ⇒  
       Q(result) && result.height > 0 )
```

Web Page Backends

```
write( toolbar.height > 10 )
```

```
for obj in results:
```

```
write( result.y > 10 ⇒  
       Q(result) && result.height > 0 )
```

Future Work

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Backend code (Python, PHP, ...)

Other platforms (Android, iOS...)

User studies with designers

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University of Utah Computer Science



University of Utah Computer Science



Exciting city in the middle of beautiful nature

Large & growing PL, compilers group



J. Regehr



Z. Rakamaric



G. Gopalakrishnan



P. Panчекha



P. Sadayappan



M. Hall



M. Flatt

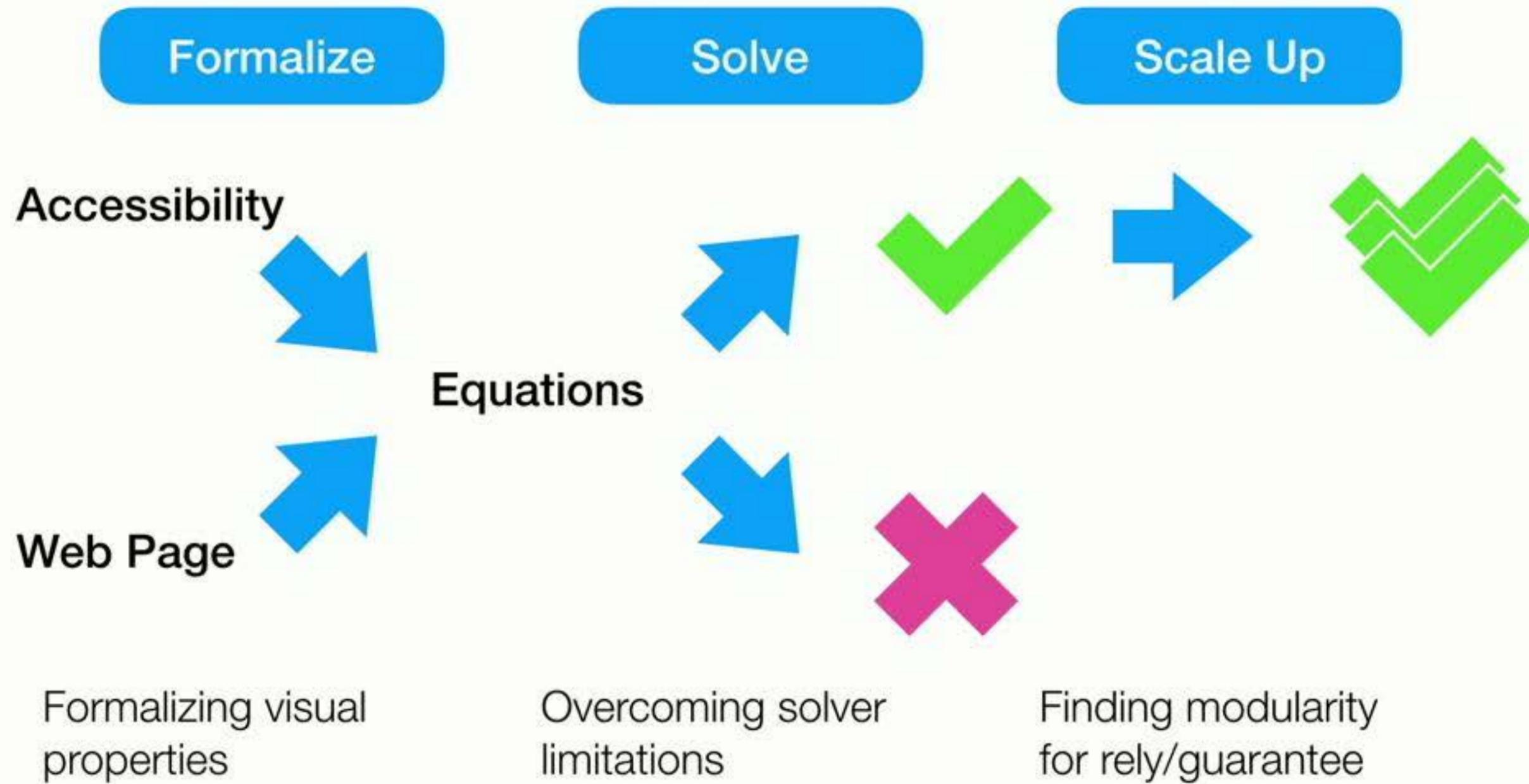
University of Utah Computer Science



Exciting city in the middle of beautiful nature

Large & growing PL, compilers group

Thank You!



cassius.uwplse.org

